

Int  
Alg

# 4

# Graphing Linear Equations and Functions

- 4.1 Plot Points in a Coordinate Plane
- 4.2 Graph Linear Equations
- 4.3 Graph Using Intercepts
- 4.4 Find Slope and Rate of Change
- 4.5 Graph Using Slope-Intercept Form
- 4.6 Model Direct Variation
- 4.7 Graph Linear Functions

## Before

In previous chapters, you learned the following skills, which you'll use in Chapter 4: graphing functions and writing equations and functions.

## Prerequisite Skills

### VOCABULARY CHECK

Copy and complete the statement.

1. The set of inputs of a function is called the ? of the function. The set of outputs of a function is called the ? of the function.
2. A(n) ? uses division to compare two quantities.

### SKILLS CHECK

Graph the function. (Review p. 43 for 4.1–4.7.)

3.  $y = x + 6$ ; domain: 0, 2, 4, 6, and 8
4.  $y = 2x + 1$ ; domain: 0, 1, 2, 3, and 4
5.  $y = \frac{2}{3}x$ ; domain: 0, 3, 6, 9, and 12
6.  $y = x - \frac{1}{2}$ ; domain: 1, 2, 3, 4, and 5
7.  $y = x - 4$ ; 5, 6, 7, and 9
8.  $y = \frac{1}{2}x + 1$ ; 2, 4, 6, and 8

Write the equation so that  $y$  is a function of  $x$ . (Review p. 184 for 4.5.)

9.  $6x + 4y = 16$
10.  $x + 2y = 5$
11.  $-12x + 6y = -12$

**@HomeTutor** Prerequisite skills practice at [classzone.com](http://classzone.com)

## Now

In Chapter 4, you will apply the big ideas listed below and reviewed in the Chapter Summary on page 270. You will also use the key vocabulary listed below.

## Big Ideas

- 1 Graphing linear equations and functions using a variety of methods
- 2 Recognizing how changes in linear equations and functions affect their graphs
- 3 Using graphs of linear equations and functions to solve real-world problems

### KEY VOCABULARY

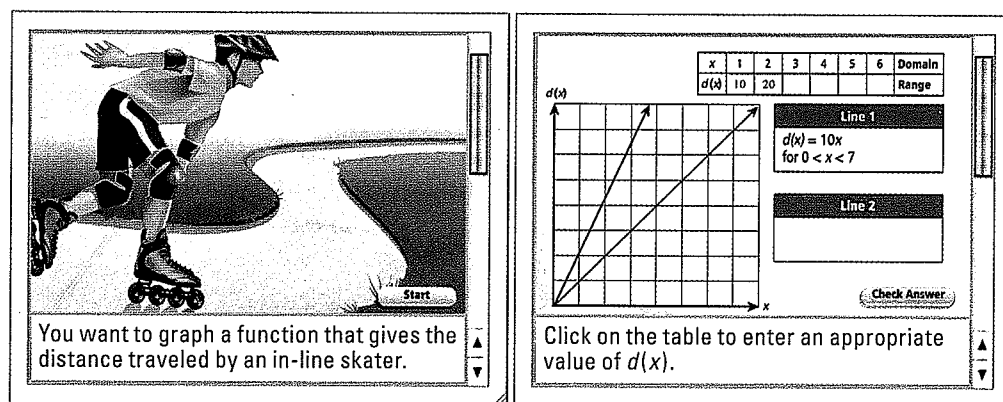
- quadrant, p. 206
- standard form of a linear equation, p. 216
- linear function, p. 217
- x-intercept, p. 225
- y-intercept, p. 225
- slope, p. 235
- rate of change, p. 237
- slope-intercept form, p. 244
- parallel, p. 246
- direct variation, p. 253
- constant of variation, p. 253
- function notation, p. 262
- family of functions, p. 263
- parent linear function, p. 263

## Why?

You can graph linear functions to solve problems involving distance. For example, you can graph a linear function to find the time it takes and in-line skater to travel a particular distance at a particular speed.

## Animated Algebra

The animation illustrated below for Exercise 41 on page 267 helps you answer this question: How can you graph a function that models the distance an in-line skater travels over time?



You want to graph a function that gives the distance traveled by an in-line skater.

x	1	2	3	4	5	6	Domain
d(x)	10	20					Range

Line 1  
 $d(x) = 10x$   
for  $0 < x < 7$

Line 2

Check Answer

Click on the table to enter an appropriate value of  $d(x)$ .

Animated Algebra at [classzone.com](http://classzone.com)

Other animations for Chapter 4: pages 207, 216, 226, 238, 245, and 254

# 4.1 EXERCISES

## HOMWORK KEY

- = WORKED-OUT SOLUTIONS on p. WS7 for Exs. 15, 25, and 37
- ★ = STANDARDIZED TEST PRACTICE Exs. 2, 13, 23, 33, and 41
- ◆ = MULTIPLE REPRESENTATIONS Ex. 40

### SKILL PRACTICE

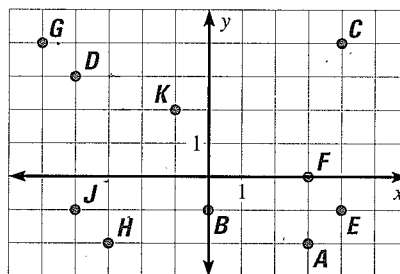
- VOCABULARY** What is the  $x$ -coordinate of the point  $(5, -3)$ ? What is the  $y$ -coordinate?
- ★ **WRITING** One of the coordinates of a point is negative while the other is positive. Can you determine the quadrant in which the point lies? *Explain.*

#### EXAMPLE 1

on p. 206  
for Exs. 3–13

#### NAMING POINTS Give the coordinates of the point.

- |       |       |
|-------|-------|
| 3. A  | 4. B  |
| 5. C  | 6. D  |
| 7. E  | 8. F  |
| 9. G  | 10. H |
| 11. J | 12. K |



- ★ **MULTIPLE CHOICE** A point is located 3 units to the left of the origin and 6 units up. What are the coordinates of the point?

- (A)  $(3, 6)$     
  (B)  $(-3, 6)$     
  (C)  $(6, 3)$     
  (D)  $(6, -3)$

#### EXAMPLE 2

on p. 207  
for Exs. 14–22

#### PLOTTING POINTS Plot the point in a coordinate plane. Describe the location of the point.

- |                 |   |                 |                  |
|-----------------|---|-----------------|------------------|
| 14. $P(5, 5)$   | <input checked="" type="radio"/> 15. $Q(-1, 5)$ | 16. $R(-3, 0)$  | 17. $S(0, 0)$    |
| 18. $T(-3, -4)$ | 19. $U(0, 6)$                                   | 20. $V(1.5, 4)$ | 21. $W(3, -2.5)$ |

- ERROR ANALYSIS** Describe and correct the error in describing the location of the point  $W(6, -6)$ .

Point  $W(6, -6)$  is 6 units to the left of the origin and 6 units up.

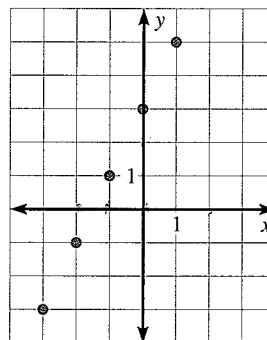


#### EXAMPLE 3

on p. 207  
for Exs. 23–27

- ★ **MULTIPLE CHOICE** Which number is in the range of the function whose graph is shown?

- (A)  $-2$     
  (B)  $-1$   
 (C)  $0$     
  (D)  $2$



**GRAPHING FUNCTIONS** Graph the function with the given domain. Then identify the range of the function.

24.  $y = -x + 1$ ; domain:  $-2, -1, 0, 1, 2$

25.  $y = 2x - 5$ ; domain:  $-2, -1, 0, 1, 2$

26.  $y = -\frac{2}{3}x - 1$ ; domain:  $-6, -3, 0, 3, 6$

27.  $y = \frac{1}{2}x + 1$ ; domain:  $-6, -4, -2, 0, 2$

28. **GEOMETRY** Plot the points  $W(-4, -2)$ ,  $X(-4, 4)$ ,  $Y(4, 4)$ , and  $Z(4, -2)$  in a coordinate plane. Connect the points in order. Connect point  $Z$  to point  $W$ . Identify the resulting figure. Find its perimeter and area.

**REASONING** Without plotting the point, tell whether it is in Quadrant I, II, III, or IV. Explain your reasoning.

29.  $(4, -11)$

30.  $(40, -40)$

31.  $(-18, 15)$

32.  $(-32, -22)$

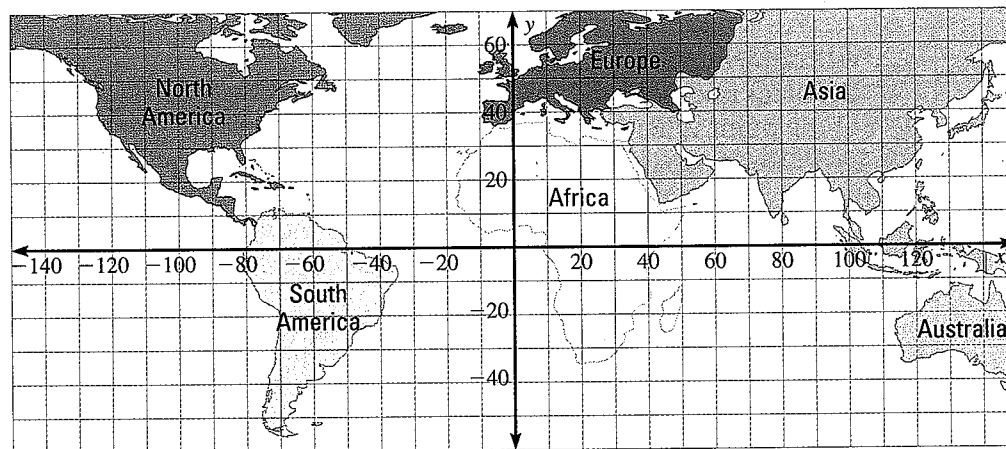
33. **★ WRITING** Explain how can you tell by looking at the coordinates of a point whether the point is on the  $x$ -axis or on the  $y$ -axis.

34. **REASONING** Plot the point  $J(-4, 3)$  in a coordinate plane. Plot three additional points in the same coordinate plane so that each of the four points lies in a different quadrant and the figure formed by connecting the points is a square. Explain how you located the points.

35. **CHALLENGE** Suppose the point  $(a, b)$  lies in Quadrant IV. Describe the location of the following points:  $(b, a)$ ,  $(2a, -2b)$ , and  $(-b, -a)$ . Explain your reasoning.

## PROBLEM SOLVING

36. **ASTRONAUT PHOTOGRAPHY** Astronauts use a coordinate system to describe the locations of objects they photograph from space. The  $x$ -axis is the equator,  $0^\circ$  latitude. The  $y$ -axis is the prime meridian,  $0^\circ$  longitude. The names and coordinates of some lakes photographed from space are given. Use the map to determine on which continent each lake is located.



a. Lake Kulundinskoye:  $(80, 53)$

b. Lake Champlain:  $(-73, 45)$

c. Lake Van:  $(43, 39)$

d. Lake Viedma:  $(-73, -50)$

e. Lake Saint Clair:  $(-83, 43)$

f. Starnberger Lake:  $(12, 48)$

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**EXAMPLE 4**  
on p. 208  
for Exs. 37–39

37. **RECORD TEMPERATURES** The table shows the record low temperatures (in degrees Fahrenheit) for Odessa, Texas, for each day in the first week of February. *Explain* how you know the table represents a function. Graph the data from the table.

<b>Day in February</b>	1	2	3	4	5	6	7
<b>Record low (degrees Fahrenheit)</b>	-8	-11	10	8	10	9	11

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38. **STOCK VALUE** The table shows the change in value (in dollars) of a stock over five days.

<b>Day</b>	1	2	3	4	5
<b>Change in value (dollars)</b>	-0.30	0.10	0.15	0.35	0.11

- a. *Explain* how you know the table represents a function. Graph the data from the table.
- b. *Describe* any trend in the change in value of the stock.
39. **MULTI-STEP PROBLEM** The difference between what the federal government collects and what it spends during a fiscal year is called the federal surplus or deficit. The table shows the federal surplus or deficit (in billions of dollars) in the 1990s. (A negative number represents a deficit.)

<b>Years since 1990</b>	0	1	2	3	4	5	6	7	8	9
<b>Surplus or deficit (billions)</b>	-221	-269	-290	-255	-203	-164	-108	-22	69	126

- a. Graph the function represented by the table.
- b. What conclusions can you make from the graph?
40. **MULTIPLE REPRESENTATIONS** Low-density lipoproteins (LDL) transport cholesterol in the bloodstream throughout the body. A high LDL number is associated with an increased risk of cardiovascular disease. A patient's LDL number in 1999 was 189 milligrams per deciliter (mg/dL). To lower that number, the patient went on a diet. The annual LDL numbers for the patient in years after 1999 are 169, 154, 145, 139, and 136.

<b>Years since 1999</b>	1	2	?	?	?
<b>Changes in LDL (mg/dL)</b>	-20	-15	?	?	?

- a. **Making a Table** Use the given information to copy and complete the table that shows the change in the patient's LDL number since 1999.
- b. **Drawing a Graph** Graph the ordered pairs from the table.
- c. **Describing in Words** Based on the graph, what can you conclude about the diet's effectiveness in lowering the patient's LDL number?

41. ★ **EXTENDED RESPONSE** In a scientific study, researchers asked men to report their heights and weights. Then the researchers measured the actual heights and weights of the men. The data for six men are shown in the table. One row of the table represents the data for one man.

Height (inches)			Weight (pounds)		
Reported	Measured	Difference	Reported	Measured	Difference
70	68	$70 - 68 = 2$	154	146	$154 - 146 = 8$
70	67.5	?	141	143	?
78.5	77.5	?	165	168	?
68	69	?	146	143	?
71	72	?	220	223	?
70	70	?	176	176	?

- a. **Calculate** Copy and complete the table.
- b. **Graph** For each participant, write an ordered pair  $(x, y)$  where  $x$  is the difference of the reported and measured heights and  $y$  is the difference of the reported and measured weights. Then plot the ordered pairs in a coordinate plane.
- c. **CHALLENGE** What does the origin represent in this situation?
- d. **CHALLENGE** Which quadrant has the greatest number of points? *Explain* what it means for a point to be in that quadrant.

## MIXED REVIEW

Evaluate the expression.

42.  $4 + 2x^2$  when  $x = 6$  (p. 2)

43.  $6 \cdot 2a^2$  when  $a = 3$  (p. 2)

44.  $4 + 2(-7) + 3$  (p. 8)

45.  $3(35 - 18)$  (p. 8)

Use the distributive property to write an equivalent expression. (p. 96)

46.  $6(x + 20)$

47.  $3x(x + 9)$

48.  $-(4 - 5y)$

49. **TRAVEL** You are traveling on the highway at an average speed of 55 miles per hour. How long will it take you to drive 66 miles? (p. 168)

Write the equation so that  $y$  is a function of  $x$ . (p. 184)

50.  $4x + y = 6$

51.  $x + 7y = 14$

52.  $4(y - 6x) = 12$

Tell whether the pairing is a function. (p. 35)

53.

Input	-5	-4	-3	-2
Output	-2	0	2	4

54.

Input	-1	0	1	2
Output	10	10	4	1

PREVIEW  
Prepare for  
Lesson 4.2  
in Exs. 50–54.

## Extension

Use after Lesson 4.1

# Perform Transformations

**GOAL** Perform and describe transformations in a coordinate plane.

### Key Vocabulary

- transformation
- translation
- vertical stretch or shrink
- reflection

For a given set of points, a **transformation** produces an image by applying a rule to the coordinates of the points. Some types of transformations are *translations*, *vertical stretches*, *vertical shrinks*, and *reflections*.

A **translation** moves every point in a figure the same distance in the same direction either horizontally, vertically, or both. You can describe translations algebraically.

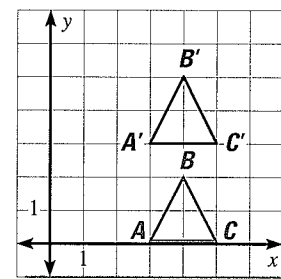
**Horizontal translation:**  $(x, y) \rightarrow (x + h, y)$       **Vertical translation:**  $(x, y) \rightarrow (x, y + k)$

### EXAMPLE 1 Perform a translation

The transformation  $(x, y) \rightarrow (x, y + 3)$  moves  $\triangle ABC$  up 3 units.

Original	Image
$A(3, 0)$	$\rightarrow A'(3, 3)$
$B(4, 2)$	$\rightarrow B'(4, 5)$
$C(5, 0)$	$\rightarrow C'(5, 3)$

The result of the transformation is  $\triangle A'B'C'$ .



### READ TRANSFORMATIONS

If a transformation is performed on a point  $A$ , the new location of point  $A$  is indicated by  $A'$  (read "A prime").

A **vertical stretch or shrink** moves every point in a figure away from the  $x$ -axis (a vertical stretch) or toward the  $x$ -axis (a vertical shrink), while points on the  $x$ -axis remain fixed. A **reflection** flips a figure in a line. You can describe vertical stretches and shrinks with or without reflection in the  $x$ -axis algebraically.

**Vertical stretch:**  
 $(x, y) \rightarrow (x, ay)$  where  $a > 1$

**Vertical shrink:**  
 $(x, y) \rightarrow (x, ay)$  where  $0 < a < 1$

**Vertical stretch with reflection in the  $x$ -axis:**  
 $(x, y) \rightarrow (x, ay)$  where  $a < -1$

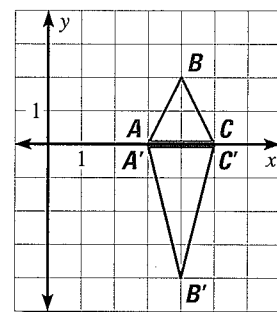
**Vertical shrink with reflection in the  $x$ -axis:**  
 $(x, y) \rightarrow (x, ay)$  where  $-1 < a < 0$

### EXAMPLE 2 Perform a vertical stretch with reflection

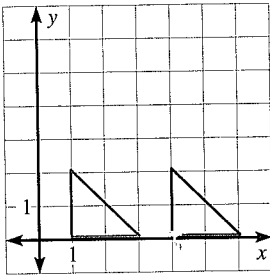
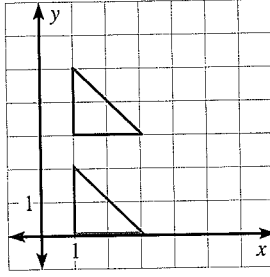
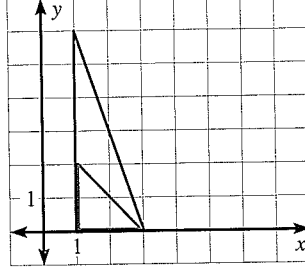
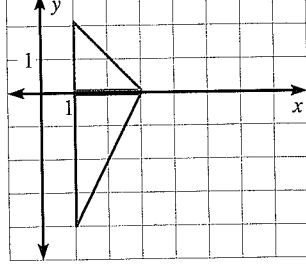
The transformation  $(x, y) \rightarrow (x, -2y)$  vertically stretches  $\triangle ABC$  and reflects it in the  $x$ -axis.

Original	Image
$A(3, 0)$	$\rightarrow A'(3, 0)$
$B(4, 2)$	$\rightarrow B'(4, -4)$
$C(5, 0)$	$\rightarrow C'(5, 0)$

The result of the transformation is  $\triangle A'B'C'$ .



Identifying Transformations

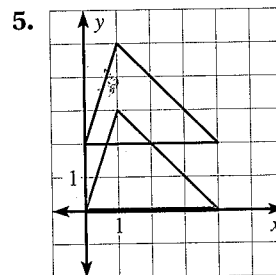
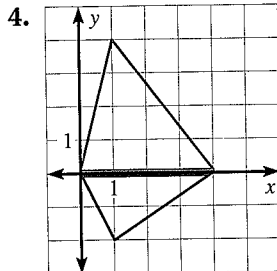
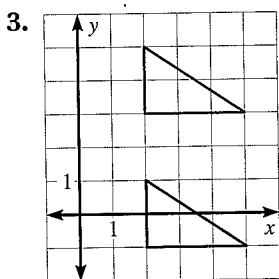
Translation		Vertical stretch or shrink	
<p><b>Horizontal</b> <math>(x, y) \rightarrow (x + h, y)</math></p> 	<p><b>Vertical</b> <math>(x, y) \rightarrow (x, y + k)</math></p> 	<p><b>Without reflection</b> <math>(x, y) \rightarrow (x, ay)</math> where <math>a &gt; 0</math></p> 	<p><b>With reflection</b> <math>(x, y) \rightarrow (x, ay)</math> where <math>a &lt; 0</math></p> 

PRACTICE

- 1. VOCABULARY** Does a translation or a vertical stretch always produce a figure that is the same size and shape as the original figure? *Explain.*
- 2. ★ WRITING** Describe the vertical shrink  $(x, y) \rightarrow (x, \frac{1}{2}y)$  in words.

EXAMPLES  
1 and 2  
on p. 213  
for Exs. 3–14

**DESCRIBING TRANSFORMATIONS** Use words to describe the transformation of the blue figure to the red figure.



**PERFORMING TRANSFORMATIONS** Square  $ABCD$  has vertices at  $(0, 0)$ ,  $(0, 2)$ ,  $(2, 2)$ , and  $(2, 0)$ . Perform the indicated transformation. Then give the coordinates of figure  $A'B'C'D'$ .

- |   |   |   |
|---|---|---|
| 6. $(x, y) \rightarrow (x, y - 5)$      | 7. $(x, y) \rightarrow (x, y + 1)$      | 8. $(x, y) \rightarrow (x, y - 7)$          |
| 9. $(x, y) \rightarrow (x, -y)$         | 10. $(x, y) \rightarrow (x, 4y)$        | 11. $(x, y) \rightarrow (x, -\frac{1}{2}y)$ |
| 12. $(x, y) \rightarrow (x + 2, y + 3)$ | 13. $(x, y) \rightarrow (x - 1, y + 4)$ | 14. $(x, y) \rightarrow (x + 3, y)$         |
15. **★ WRITING** A square has vertices at  $(0, 0)$ ,  $(0, 3)$ ,  $(3, 3)$ , and  $(3, 0)$ . Tell how you could use a transformation to move the square so that it has new vertices at  $(0, 0)$ ,  $(0, -3)$ ,  $(3, -3)$ , and  $(3, 0)$ .

# 4.2 EXERCISES

## HOMEWORK KEY

- = WORKED-OUT SOLUTIONS on p. WS8 for Exs. 3, 11, and 37
- ★ = STANDARDIZED TEST PRACTICE Exs. 2, 10, 32, 33, 39, and 41
- ◆ = MULTIPLE REPRESENTATIONS Ex. 40

### SKILL PRACTICE

**EXAMPLE 1**  
on p. 215  
for Exs. 3–10

1. **VOCABULARY** The equation  $Ax + By = C$  represents a(n) ? provided  $B \neq 0$ .

2. **★ WRITING** Is the equation  $y = 6x + 4$  in standard form? *Explain.*

**CHECKING SOLUTIONS** Tell whether the ordered pair is a solution of the equation.

3.  $2y + x = 4$ ;  $(-2, 3)$

4.  $3x - 2y = -5$ ;  $(-1, 1)$

5.  $x = 9$ ;  $(9, 6)$

6.  $y = -7$ ;  $(-7, 0)$

7.  $-7x - 4y = 1$ ;  $(-3, -5)$

8.  $-5y - 6x = 0$ ;  $(-6, 5)$

9. **ERROR ANALYSIS** Describe and correct the error in determining whether  $(8, 11)$  is a solution of  $y - x = -3$ .

$$y - x = -3$$

$$8 - 11 = -3$$

$$-3 = -3$$

$(8, 11)$  is a solution.



10. **★ MULTIPLE CHOICE** Which ordered pair is a solution of  $6x + 3y = 18$ ?

(A)  $(-2, -10)$

(B)  $(-2, 10)$

(C)  $(2, 10)$

(D)  $(10, -2)$

**EXAMPLES 2 and 3**  
on p. 216  
for Exs. 11–25

**GRAPHING EQUATIONS** Graph the equation.

11.  $y + x = 2$

12.  $y - 2x = 5$

13.  $y - 3x = 0$

14.  $y + 4x = 1$

15.  $2y - 6x = 10$

16.  $3y + 4x = 12$

17.  $x - 2y = 3$

18.  $3x + 2y = 8$

19.  $x = 0$

20.  $y = 0$

21.  $y = -4$

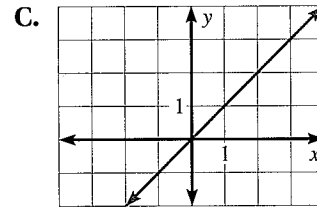
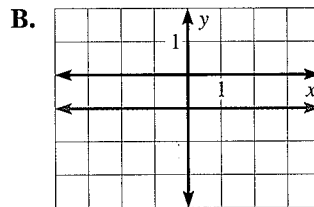
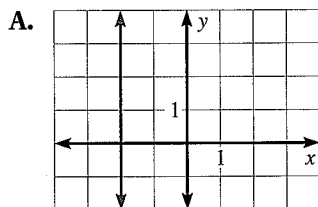
22.  $x = 2$

**MATCHING EQUATIONS WITH GRAPHS** Match the equation with its graph.

23.  $y - x = 0$

24.  $x = -2$

25.  $y = -1$



**EXAMPLE 4**  
on p. 217  
for Exs. 26–31

**GRAPHING FUNCTIONS** Graph the function with the given domain. Then identify the range of the function.

26.  $y = 3x - 2$ ; domain:  $x \geq 0$

27.  $y = -5x + 3$ ; domain:  $x \leq 0$

28.  $y = 4$ ; domain:  $x \leq 5$

29.  $y = -6$ ; domain:  $x \geq 5$

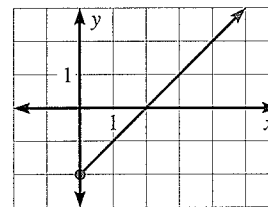
30.  $y = 2x + 3$ ; domain:  $-4 \leq x \leq 0$

31.  $y = -x - 1$ ; domain:  $-1 \leq x \leq 3$

32. **★ OPEN-ENDED** Graph  $x - y = 3$  and  $2x - 2y = 6$ . *Explain* why the equations look different but have the same graph. Find another equation that looks different from the two given equations but has the same graph.



33. ★ **MULTIPLE CHOICE** Which statement is true for the function whose graph is shown?



- (A) The domain is unrestricted.
- (B) The domain is  $x \leq -2$ .
- (C) The range is  $y \leq -2$ .
- (D) The range is  $y \geq -2$ .

34. **CHALLENGE** If  $(3, n)$  is a solution of  $Ax + 3y = 6$  and  $(n, 5)$  is a solution of  $5x + y = 20$ , what is the value of  $A$ ?

## PROBLEM SOLVING

**EXAMPLES**  
5 and 6  
on p. 218  
for Exs. 35–39

35. **BAKING** The weight  $w$  (in pounds) of a loaf of bread that a recipe yields is given by the function  $w = \frac{1}{2}f$  where  $f$  is the number of cups of flour used. You have 4 cups of flour. Graph the function and identify its domain and range. What is the weight of the largest loaf of bread you can make?

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36. **TRAVEL** After visiting relatives who live 200 miles away, your family drives home at an average speed of 50 miles per hour. Your distance  $d$  (in miles) from home is given by  $d = 200 - 50t$  where  $t$  is the time (in hours) spent driving. Graph the function and identify its domain and range. What is your distance from home after driving for 1.5 hours?

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37. **EARTH SCIENCE** The temperature  $T$  (in degrees Celsius) of Earth's crust can be modeled by the function  $T = 20 + 25d$  where  $d$  is the distance (in kilometers) from the surface.

- a. A scientist studies organisms in the first 4 kilometers of Earth's crust. Graph the function and identify its domain and range. What is the temperature at the deepest part of the section of crust?
- b. Suppose the scientist studies organisms in a section of the crust where the temperature is between  $20^\circ\text{C}$  and  $95^\circ\text{C}$ . Graph the function and identify its domain and range. How many kilometers deep is the section of crust?

38. **MULTI-STEP PROBLEM** A fashion designer orders fabric that costs \$30 per yard. The designer wants the fabric to be dyed, which costs \$100. The total cost  $C$  (in dollars) of the fabric is given by the function

$$C = 30f + 100$$

where  $f$  is the number of yards of fabric.

- a. The designer orders 3 yards of fabric. How much does the fabric cost? *Explain.*
- b. Suppose the designer can spend \$500 on fabric. How many yards of fabric can the designer buy? *Explain.*

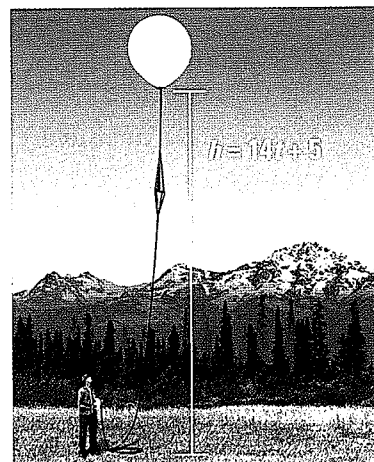


39. ★ **SHORT RESPONSE** An emergency cell phone charger requires you to turn a small crank in order to create the energy needed to recharge the phone's battery. If you turn the crank 120 times per minute, the total number  $r$  of revolutions that you turn the crank is given by

$$r = 120t$$

where  $t$  is the time (in minutes) spent turning the crank.

- Graph the function and identify its domain and range.
  - Identify the domain and range if you stop turning the crank after 4 minutes. *Explain* how this affects the appearance of the graph.
40. ❖ **MULTIPLE REPRESENTATIONS** The National Weather Service releases weather balloons twice daily at over 90 locations in the United States in order to collect data for meteorologists. The height  $h$  (in feet) of a balloon is a function of the time  $t$  (in seconds) after the balloon is released, as shown.



- Making a Table** Make a table showing the height of a balloon after  $t$  seconds for  $t = 0$  through  $t = 10$ .
  - Drawing a Graph** A balloon bursts after a flight of about 7200 seconds. Graph the function and identify the domain and range.
41. ★ **EXTENDED RESPONSE** Students can pay for lunch at a school in one of two ways. Students can either make a payment of \$30 per month or they can buy lunch daily for \$2.50 per lunch.
- Graph** Graph the function  $y = 30$  to represent the monthly payment plan. Using the same coordinate plane, graph the function  $y = 2.5x$  to represent the daily payment plan.
  - CHALLENGE** What are the coordinates of the point that is a solution of both functions? What does that point mean in this situation?
  - CHALLENGE** A student eats an average of 15 school lunches per month. How should the student pay, daily or monthly? *Explain.*

## MIXED REVIEW

Solve the equation.

42.  $12x = 144$  (p. 134)

44.  $5.7x - 2x = 14.8$  (p. 141)

46.  $6x - 4x + 13 = 27 - 2x$  (p. 154)

43.  $-4x = 30$  (p. 134)

45.  $x - 4(x + 13) = 26$  (p. 148)

47.  $5x - \frac{1}{4}(24 + 8x) = 2x - 5$  (p. 154)

Plot the point in a coordinate plane. *Describe* the location of the point. (p. 206)

48. (3, 5)

49. (-3, 2)

50. (0, -2)

51. (-5, 0)

52. (-2, -2)

53.  $(\frac{1}{3}, 0)$

54.  $(-\frac{1}{2}, \frac{3}{4})$

55. (0, 6.2)

### PREVIEW

Prepare for  
Lesson 4.3  
in Exs. 48–55.

## 4.2 Graphing Linear Equations

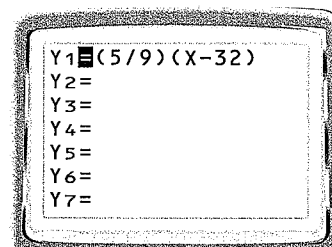
**QUESTION** How do you graph an equation on a graphing calculator?

**EXAMPLE** Use a graph to solve a problem

The formula to convert temperature from degrees Fahrenheit to degrees Celsius is  $C = \frac{5}{9}(F - 32)$ . Graph the equation. At what temperature are degrees Fahrenheit and degrees Celsius equal?

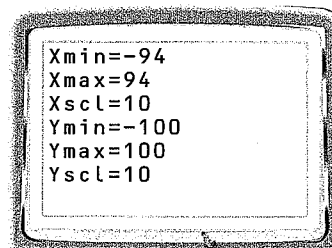
**STEP 1** Rewrite and enter equation

Rewrite the equation using  $x$  for  $F$  and  $y$  for  $C$ . Enter the equation into the **Y=** screen. Put parentheses around the fraction  $\frac{5}{9}$ .



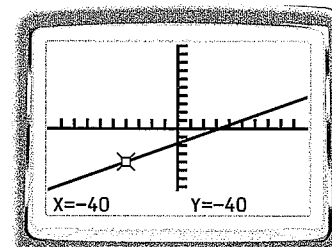
**STEP 2** Set window

The screen is a “window” that lets you look at part of a coordinate plane. Press **WINDOW** to set the borders of the graph. A friendly window for this equation is  $-94 \leq x \leq 94$  and  $-100 \leq y \leq 100$ .



**STEP 3** Graph and trace equation

Press **TRACE** and use the left and right arrows to move the cursor along the graph until the  $x$ -coordinate and  $y$ -coordinate are equal. From the graph, you can see that degrees Fahrenheit and degrees Celsius are equal at  $-40$ .



**PRACTICE**

Graph the equation. Find the unknown value in the ordered pair.

- $y = 8 - x$ ;  $(2.4, \underline{\quad})$
- $y = 2x + 3$ ;  $(\underline{\quad}, 0.8)$
- $y = -4.5x + 1$ ;  $(1.4, \underline{\quad})$
- SPEED OF SOUND** The speed  $s$  (in meters per second) of sound in air can be modeled by  $s = 331.1 + 0.61T$  where  $T$  is the air temperature in degrees Celsius. Graph the equation. Estimate the speed of sound when the temperature is  $20^\circ\text{C}$ .

## Extension

Use after Lesson 4.2

# Identify Discrete and Continuous Functions

**GOAL** Graph and classify discrete and continuous functions.

### Key Vocabulary

- discrete function
- continuous function

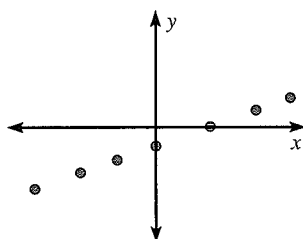
The graph of a function can consist of individual points, as in the graph in Example 3 on page 207. The graph of a function can also be a line or a part of a line with no breaks, as in the graph in Example 4 on page 217.

### KEY CONCEPT

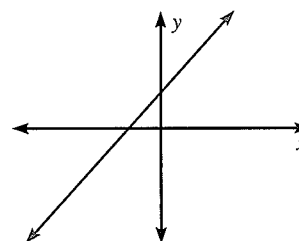
*For Your Notebook*

#### Identifying Discrete and Continuous Functions

A **discrete function** has a graph that consists of isolated points.



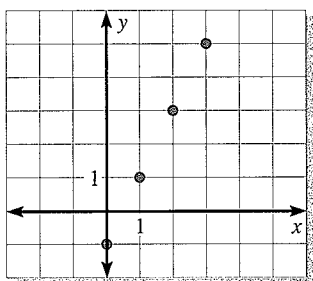
A **continuous function** has a graph that is unbroken.



### EXAMPLE 1 Graph and classify a function

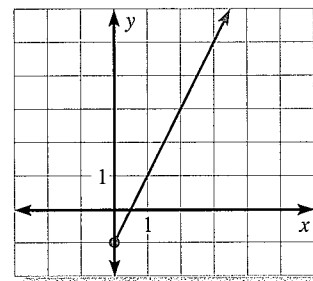
Graph the function  $y = 2x - 1$  with the given domain. Classify the function as discrete or continuous.

a. Domain:  $x = 0, 1, 2, 3$



The graph consists of individual points, so the function is discrete.

b. Domain:  $x \geq 0$



The graph is unbroken, so the function is continuous.

**GRAPHS** As a general rule, you can tell that a function is continuous if you do not have to lift your pencil from the paper to draw its graph, as in part (b) of Example 1.

**EXAMPLE 2** Classify and graph a real-world function

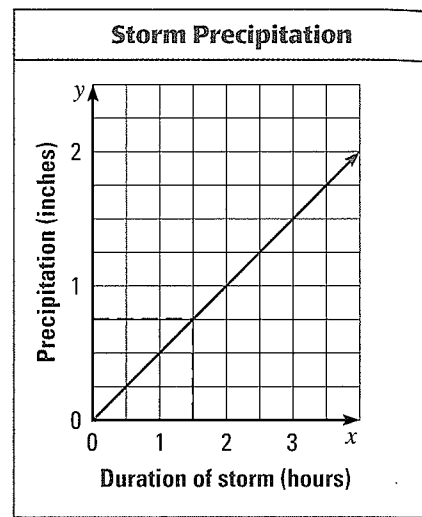
Tell whether the function represented by the table is discrete or continuous. Explain. If continuous, graph the function and find the value of  $y$  when  $x = 1.5$ .

Duration of storm (hours), $x$	1	2	3
Amount of rain (inches), $y$	0.5	1	1.5

**Solution**

Although the table shows the amount of rain that has fallen after whole numbers of hours only, it makes sense to talk about the amount of rain after any amount of time during the storm. So, the table represents a continuous function.

The graph of the function is shown. To find the value of  $y$  when  $x = 1.5$ , start at 1.5 on the  $x$ -axis, move up to the graph, and move over to the  $y$ -axis. The  $y$ -value is about 0.75. So, about 0.75 inch of rain has fallen after 1.5 hours.

**PRACTICE**

**EXAMPLE 1**  
on p. 223  
for Exs. 1–6

Graph the function with the given domain. Classify the function as discrete or continuous.

- $y = -2x + 3$ ; domain:  $-2, -1, 0, 1, 2$
- $y = x$ ; domain: all real numbers
- $y = -\frac{1}{3}x + 1$ ; domain:  $-12, -6, 0, 6, 12$
- $y = 0.5x$ ; domain:  $-2, -1, 0, 1, 2$
- $y = 3x - 4$ ; domain:  $x \leq 0$
- $y = \frac{2}{3}x + \frac{1}{3}$ ; domain:  $x \geq -2$

**EXAMPLE 2**  
on p. 224  
for Exs. 7–9

Tell whether the function represented by the table is discrete or continuous. Explain. If continuous, graph the function and find the value of  $y$  when  $x = 3.5$ . Round your answer to the nearest hundredth.

7.

Number of DVD rentals, $x$	1	2	3	4
Cost of rentals (dollars), $y$	4.50	9.00	13.50	18.00

8.

Hours since 12 P.M., $x$	2	4	6	8
Distance driven (miles), $y$	100	200	300	400

9.

Volume of water (cubic inches), $x$	3	6	9	12
Approximate weight of water (pounds), $y$	0.1	0.2	0.3	0.4



# 4.3 EXERCISES

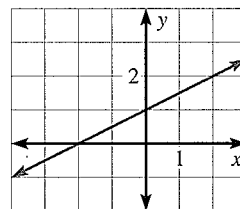
## HOMEWORK KEY

- = WORKED-OUT SOLUTIONS on p. WS8 for Exs. 21 and 47
- ★ = STANDARDIZED TEST PRACTICE Exs. 2, 37, 41, 49, and 50
- ◆ = MULTIPLE REPRESENTATIONS Ex. 44

### SKILL PRACTICE

1. **VOCABULARY** Copy and complete: The      of the graph of an equation is the value of  $x$  when  $y$  is zero.
2. ★ **WRITING** What are the  $x$ -intercept and the  $y$ -intercept of the line passing through the points  $(0, 3)$  and  $(-4, 0)$ ? *Explain.*
3. **ERROR ANALYSIS** Describe and correct the error in finding the intercepts of the line shown.

The  $x$ -intercept is 1,  
and the  $y$ -intercept is  $-2$ .



**EXAMPLE 1**  
on p. 225  
for Exs. 4–15

**FINDING INTERCEPTS** Find the  $x$ -intercept and the  $y$ -intercept of the graph of the equation.

- |                     |                          |                             |
|---------------------|--------------------------|-----------------------------|
| 4. $5x - y = 35$    | 5. $3x - 3y = 9$         | 6. $-3x + 9y = -18$         |
| 7. $4x + y = 4$     | 8. $2x + y = 10$         | 9. $2x - 8y = 24$           |
| 10. $3x + 0.5y = 6$ | 11. $0.2x + 3.2y = 12.8$ | 12. $y = 2x + 24$           |
| 13. $y = -14x + 7$  | 14. $y = -4.8x + 1.2$    | 15. $y = \frac{3}{5}x - 12$ |

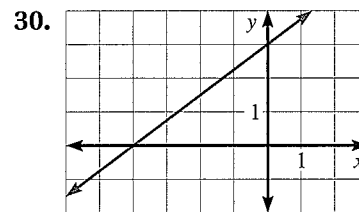
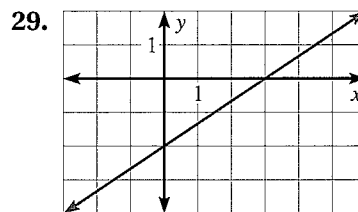
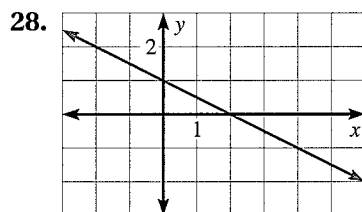
**EXAMPLE 2**  
on p. 226  
for Exs. 16–27

**GRAPHING LINES** Graph the equation. Label the points where the line crosses the axes.

- |                     |                     |                                      |
|---------------------|---------------------|--------------------------------------|
| 16. $y = x + 3$     | 17. $y = x - 2$     | 18. $y = 4x - 8$                     |
| 19. $y = 5 + 10x$   | 20. $y = -2 + 8x$   | 21. $y = -4x + 3$                    |
| 22. $3x + y = 15$   | 23. $x - 4y = 18$   | 24. $8x - 5y = 80$                   |
| 25. $-2x + 5y = 15$ | 26. $0.5x + 3y = 9$ | 27. $y = \frac{1}{2}x + \frac{1}{4}$ |

**EXAMPLE 3**  
on p. 226  
for Exs. 28–30

**USING GRAPHS TO FIND INTERCEPTS** Identify the  $x$ -intercept and the  $y$ -intercept of the graph.



**USING INTERCEPTS** Draw the line that has the given intercepts.

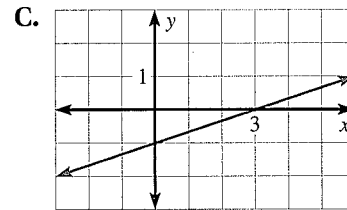
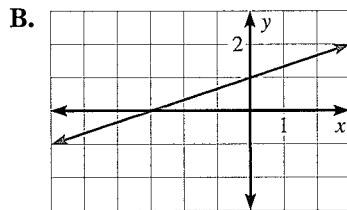
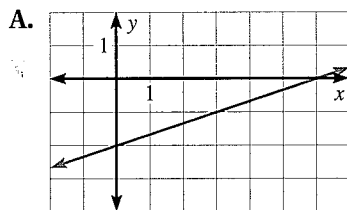
31.  $x$ -intercept: 3  
 $y$ -intercept: 5
32.  $x$ -intercept:  $-2$   
 $y$ -intercept: 4
33.  $x$ -intercept:  $-5$   
 $y$ -intercept: 6
34.  $x$ -intercept: 9  
 $y$ -intercept:  $-1$
35.  $x$ -intercept:  $-8$   
 $y$ -intercept:  $-11$
36.  $x$ -intercept:  $-2$   
 $y$ -intercept:  $-6$

37. **★ MULTIPLE CHOICE** The  $x$ -intercept of the graph of  $Ax + 5y = 20$  is 2. What is the value of  $A$ ?

- (A) 2                      (B) 5                      (C) 7.5                      (D) 10

**MATCHING EQUATIONS WITH GRAPHS** Match the equation with its graph.

38.  $2x - 6y = 6$                       39.  $2x - 6y = -6$                       40.  $2x - 6y = 12$



41. **★ WRITING** Is it possible for a line *not* to have an  $x$ -intercept? Is it possible for a line *not* to have a  $y$ -intercept? *Explain.*
42. **REASONING** Consider the equation  $3x + 5y = k$ . What values could  $k$  have so that the  $x$ -intercept and the  $y$ -intercept of the equation's graph would both be integers? *Explain.*
43. **CHALLENGE** If  $a \neq 0$ , find the intercepts of the graph of  $y = ax + b$  in terms of  $a$  and  $b$ .

**PROBLEM SOLVING**

**EXAMPLES**  
**4 and 5**  
 on pp. 227–228  
 for Exs. 44–47

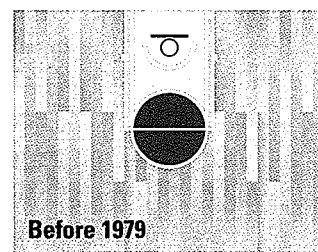
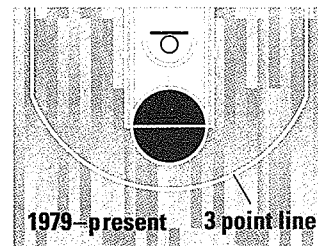
44. **◆ MULTIPLE REPRESENTATIONS** The perimeter of a rectangular park is 72 feet. Let  $x$  be the park's width (in feet) and let  $y$  be its length (in feet).
- a. **Writing an Equation** Write an equation for the perimeter.
- b. **Drawing a Graph** Find the intercepts of the graph of the equation you wrote. Then graph the equation.

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45. **RECYCLING** In one state, small bottles have a refund value of \$.04 each, and large bottles have a refund value of \$.08 each. Your friend returns both small and large bottles and receives \$.56. This situation is given by  $4x + 8y = 56$  where  $x$  is the number of small bottles and  $y$  is the number of large bottles.
- a. Find the intercepts of the graph of the equation. Graph the equation.
- b. Give three possibilities for the number of each size bottle your friend could have returned.

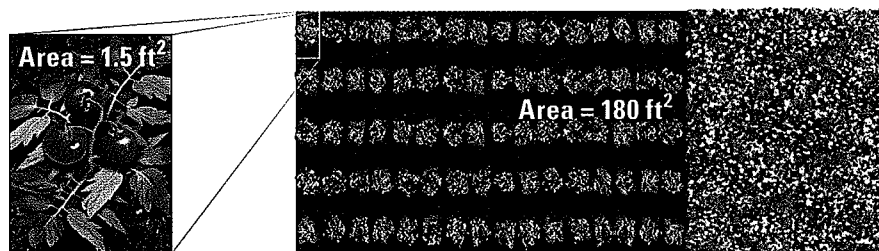
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46. **MULTI-STEP PROBLEM** Before 1979, there was no 3-point shot in professional basketball; players could score only 2-point field goals and 1-point free throws. In a game before 1979, a team scored a total of 128 points. This situation is given by the equation  $2x + y = 128$  where  $x$  is the possible number of field goals and  $y$  is the possible number of free throws.



- Find the intercepts of the graph of the equation. Graph the equation.
- What do the intercepts mean in this situation?
- What are three possible numbers of field goals and free throws the team could have scored?
- If the team made 24 free throws, how many field goals were made?

47. **COMMUNITY GARDENS** A family has a plot in a community garden. The family is going to plant vegetables, flowers, or both. The diagram shows the area used by one vegetable plant and the area of the entire plot. The area  $f$  (in square feet) of the plot left for flowers is given by  $f = 180 - 1.5v$  where  $v$  is the number of vegetable plants the family plants.



- Find the intercepts of the graph of the function and state what the intercepts represent.
  - Graph the function and identify its domain and range.
  - The family decides to plant 80 vegetable plants. How many square feet are left to plant flowers?
48. **CAR SHARING** A member of a car-sharing program can use a car for \$6 per hour and \$.50 per mile. The member uses the car for one day and is charged \$44. This situation is given by

$$6t + 0.5d = 44$$

where  $t$  is the time (in hours) the car is used and  $d$  is the distance (in miles) the car is driven. Give three examples of the number of hours the member could have used the car and the number of miles the member could have driven the car.

49. **★ SHORT RESPONSE** A humidifier is a device used to put moisture into the air by turning water to vapor. A humidifier has a tank that can hold 1.5 gallons of water. The humidifier can disperse the water at a rate of 0.12 gallon per hour. The amount of water  $w$  (in gallons) left in the humidifier after  $t$  hours of use is given by the function

$$w = 1.5 - 0.12t.$$

After how many hours of use will you have to refill the humidifier? Explain how you found your answer.

50. ★ **EXTENDED RESPONSE** You borrow \$180 from a friend who doesn't charge you interest. You work out a payment schedule in which you will make weekly payments to your friend. The balance  $B$  (in dollars) of the loan is given by the function  $B = 180 - pn$  where  $p$  is the weekly payment and  $n$  is the number of weeks you make payments.

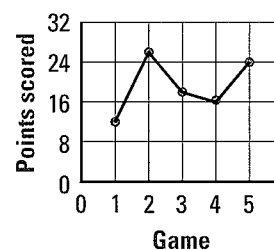
- Interpret** Without finding the intercepts, state what they represent.
- Graph** Graph the function if you make weekly payments of \$20.
- Identify** Find the domain and range of the function in part (b). How long will it take to pay back your friend?
- CHALLENGE** Suppose you make payments of \$20 for three weeks. Then you make payments of \$15 until you have paid your friend back. How does this affect the graph? How many payments do you make?

## MIXED REVIEW

### REVIEW GRAPHS

For help with line graphs, see p. 934.

In Exercises 51–53, use the line graph, which shows the number of points Alex scored in five basketball games. (p. 934)



- How many points did Alex score in game 4?
- In which game did Alex score the most points?
- How many more points did Alex score in game 5 than in game 1?

### PREVIEW

Prepare for Lesson 4.4 in Exs. 54–56.

Solve the proportion. (p. 168)

$$54. \frac{3}{5} = \frac{x}{30}$$

$$55. \frac{x}{x+6} = \frac{7}{6}$$

$$56. \frac{t-3}{12} = \frac{2t-2}{9}$$

## QUIZ for Lessons 4.1–4.3

Plot the point in a coordinate plane. Describe the location of the point. (p. 206)

1.  $(-7, 2)$

2.  $(0, -5)$

3.  $(2, -6)$

Graph the equation. (p. 215)

4.  $-4x - 2y = 12$

5.  $y = -5$

6.  $x = 6$

Find the  $x$ -intercept and the  $y$ -intercept of the graph of the equation. (p. 225)

7.  $y = x + 7$

8.  $y = x - 3$

9.  $y = -5x + 2$

10.  $x + 3y = 15$

11.  $3x - 6y = 36$

12.  $-2x - 5y = 22$

13. **SWIMMING POOLS** A public swimming pool that holds 45,000 gallons of water is going to be drained for maintenance at a rate of 100 gallons per minute. The amount of water  $w$  (in gallons) in the pool after  $t$  minutes is given by the function  $w = 45,000 - 100t$ . Graph the function. Identify its domain and range. How much water is in the pool after 60 minutes? How many minutes will it take to empty the pool? (p. 225)



## Lessons 4.1–4.3

**1. MULTI-STEP PROBLEM** An amusement park charges \$20 for an all-day pass and \$10 for a pass after 5 P.M. On Wednesday the amusement park collected \$1000 in pass sales. This situation can be modeled by the equation  $1000 = 20x + 10y$  where  $x$  is the number of all-day passes sold and  $y$  is the number of passes sold after 5 P.M.

- Find the  $x$ -intercept of the graph of the equation. What does it represent?
- Find the  $y$ -intercept of the graph of the equation. What does it represent?
- Graph the equation using a scale of 10 on the  $x$ - and  $y$ -axes.

**2. MULTI-STEP PROBLEM** A violin player who plays every day received a violin with new strings. Players who play every day should replace the strings on their violins every 6 months. A particular brand of strings costs \$24 per pack. The table shows the total spent  $a$  (in dollars) on replacement strings with respect to time  $t$  (in months).

$t$ (months)	$a$ (dollars)
6	24
12	48
18	72
24	96
30	120

- Explain how you know the table represents a function.
- Graph the function.

**3. OPEN-ENDED** Create a table that shows the number of minutes you think you will spend watching TV next week. Let Monday be day 1, Tuesday be day 2, and so on. Graph the data. Does the graph represent a function? *Explain.*

**4. SHORT RESPONSE** You can hike at an average rate of 3 miles per hour. Your total hiking distance  $d$  (in miles) can be modeled by the function  $d = 3t$  where  $t$  is the time (in hours) you hike. You plan on hiking for 10 hours this weekend.

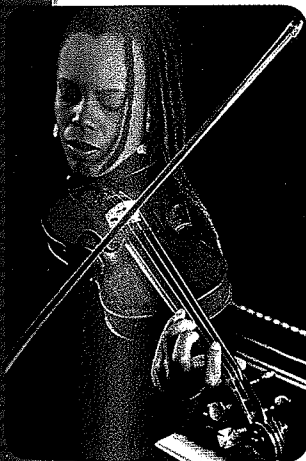
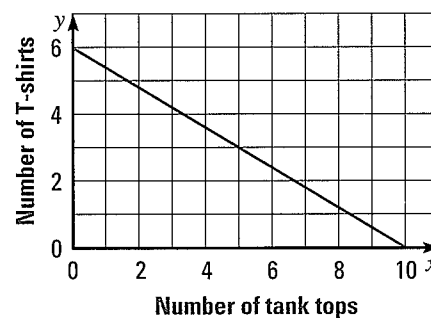
- Is the domain or range specified in the problem? *Explain.*
- Graph the function and identify its domain and range. Use the graph to find how long it takes to hike 6 miles.

**5. EXTENDED RESPONSE** The table shows the departure  $d$  (in degrees Fahrenheit) from the normal monthly temperature in New England for the first six months of 2004. For example, in month 1,  $d = -3$ . So, the average temperature was 3 degrees below the normal temperature for January.

$M$ (month)	1	2	3	4	5	6
$d$ ( $^{\circ}\text{F}$ )	-3	-1	2	2	4	-1

- Explain how you know the table represents a function.
- Graph the function and identify its domain and range.
- What does a point in Quadrant IV mean in terms of this situation?

**6. GRIDDED ANSWER** The graph shows the possible combinations of T-shirts and tank tops that you can buy with the amount of money you have. If you buy only T-shirts, how many can you buy?





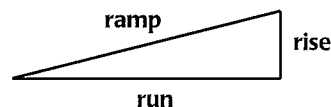
## 4.4 Slopes of Lines

**MATERIALS** • several books • two rulers

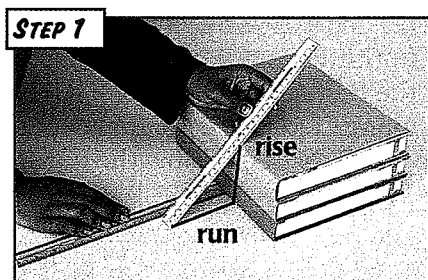
**QUESTION** How can you use algebra to describe the slope of a ramp?

You can use the ratio of the vertical rise to the horizontal run to describe the *slope* of a ramp.

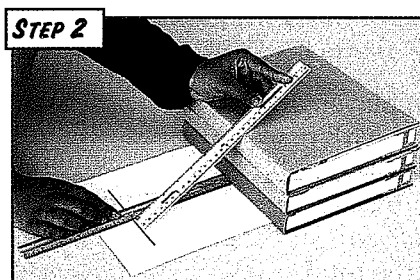
$$\text{slope} = \frac{\text{rise}}{\text{run}}$$



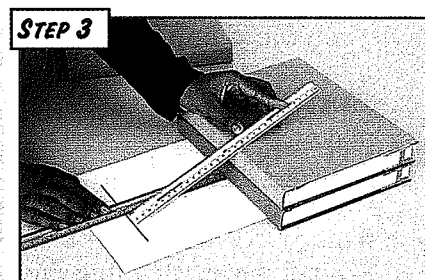
**EXPLORE** Calculate the slopes of ramps



**Make a ramp** Make a stack of three books. Use a ruler as a ramp. Measure the rise and run of the ramp, and record them in a table. Calculate and record the slope of the ramp in your table.



**Change the run** Without changing the rise, make three ramps with different runs by moving the lower end of the ruler. Measure and record the rise and run of each ramp. Calculate and record each slope.



**Change the rise** Without changing the run, make three ramps with different rises by adding or removing books. Measure and record the rise and run of each ramp. Calculate and record each slope.

**DRAW CONCLUSIONS** Use your observations to complete these exercises

*Describe* how the slope of the ramp changes given the following conditions. Give three examples that support your answer.

1. The run of the ramp increases, and the rise stays the same.
2. The rise of the ramp increases, and the run stays the same.

**In Exercises 3–5, describe the relationship between the rise and the run of the ramp.**

3. A ramp with a slope of 1
4. A ramp with a slope greater than 1
5. A ramp with a slope less than 1
6. Ramp A has a rise of 6 feet and a run of 2 feet. Ramp B has a rise of 10 feet and a run of 4 feet. Which ramp is steeper? How do you know?

# 4.4 EXERCISES

**HOMEWORK KEY**

○ = WORKED-OUT SOLUTIONS on p. WS9 for Exs. 11 and 37

★ = STANDARDIZED TEST PRACTICE Exs. 2, 17, 18, 34, and 40

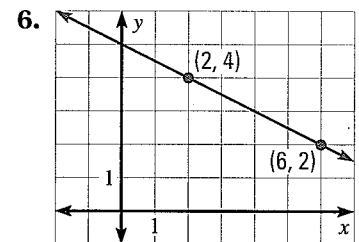
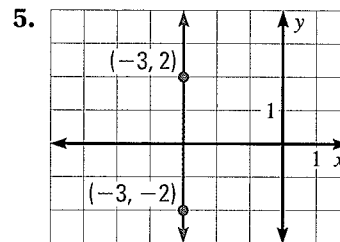
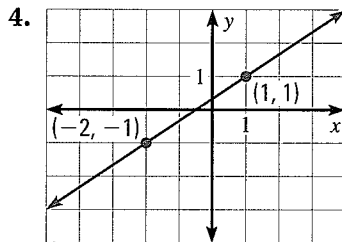
## SKILL PRACTICE

- VOCABULARY** Copy and complete: The ? of a nonvertical line is the ratio of the vertical change to the horizontal change between any two points on the line.
- ★ **WRITING** Without calculating the slope, how can you tell that the slope of the line that passes through the points  $(-5, -3)$  and  $(2, 4)$  is positive?
- ERROR ANALYSIS** Describe and correct the error in calculating the slope of the line passing through the points  $(5, 3)$  and  $(2, 6)$ .

$$m = \frac{6-3}{5-2} = \frac{3}{3} = 1$$

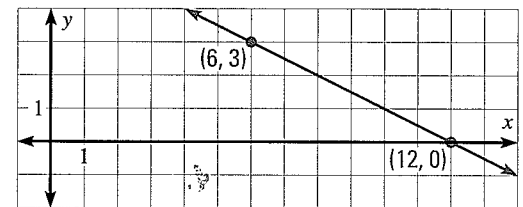
**EXAMPLES**  
1, 2, 3, and 4  
on pp. 235–236  
for Exs. 4–18

**FINDING SLOPE** Tell whether the slope of the line is *positive*, *negative*, *zero*, or *undefined*. Then find the slope if it exists.



7. **ERROR ANALYSIS** Describe and correct the error in calculating the slope of the line shown.

$$m = \frac{12-6}{0-3} = \frac{6}{-3} = -2$$



**FINDING SLOPE** Find the slope of the line that passes through the points.

- $(-2, -1)$  and  $(4, 5)$
- $(-3, -2)$  and  $(-3, 6)$
- $(5, -3)$  and  $(-5, -3)$
- $(1, 3)$  and  $(3, -2)$
- $(-3, 4)$  and  $(4, 1)$
- $(1, -3)$  and  $(7, 3)$
- $(0, 0)$  and  $(0, -6)$
- $(-9, 1)$  and  $(1, 1)$
- $(-10, -2)$  and  $(-8, 8)$
- ★ **MULTIPLE CHOICE** The slope of the line that passes through the points  $(-2, -3)$  and  $(8, -3)$  is ?.  
 (A) positive      (B) negative      (C) zero      (D) undefined
- ★ **MULTIPLE CHOICE** What is the slope of the line that passes through the points  $(7, -9)$  and  $(-13, -6)$ ?  
 (A)  $-\frac{3}{20}$       (B)  $\frac{3}{20}$       (C)  $\frac{3}{4}$       (D)  $\frac{5}{2}$

**EXAMPLE 5**  
 on p. 237  
 for Exs. 19–20

19. **MOVIE RENTALS** The table shows the number of days you keep a rented movie before returning it and the total cost of renting the movie. Find the rate of change in cost with respect to time and interpret its meaning.

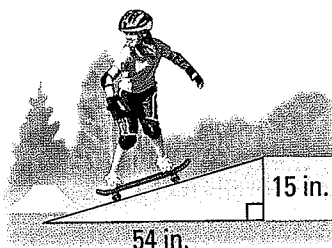
Time (days)	4	5	6	7
Total cost (dollars)	6.00	8.25	10.50	12.75

20. **AMUSEMENT PARK** The table shows the amount of time spent at an amusement park and the admission fee the park charges. Find the rate of change in the fee with respect to time spent at the park and interpret its meaning.

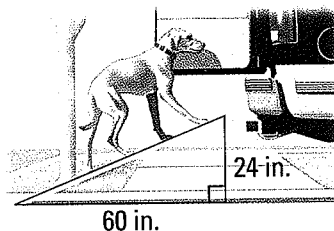
Time (hours)	4	5	6
Admission fee (dollars)	34.99	34.99	34.99

**FINDING SLOPE** Find the slope of the object. Round to the nearest tenth.

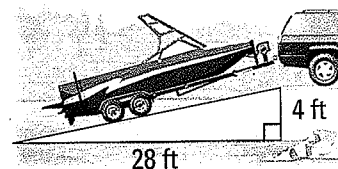
21. Skateboard ramp



22. Pet ramp



23. Boat ramp



In Exercises 24–32, use the example below to find the value of  $x$  or  $y$  so that the line passing through the given points has the given slope.

**EXAMPLE** Find a coordinate given the slope of a line

Find the value of  $x$  so that the line that passes through the points  $(2, 3)$  and  $(x, 9)$  has a slope of  $\frac{3}{2}$ .

**Solution**

Let  $(x_1, y_1) = (2, 3)$  and  $(x_2, y_2) = (x, 9)$ .

$$m = \frac{y_2 - y_1}{x_2 - x_1} \quad \text{Write formula for slope.}$$

$$\frac{3}{2} = \frac{9 - 3}{x - 2} \quad \text{Substitute values.}$$

$$3(x - 2) = 2(9 - 3) \quad \text{Cross products property}$$

$$3x - 6 = 12 \quad \text{Simplify.}$$

$$x = 6 \quad \text{Solve for } x.$$

24.  $(x, 4), (6, -1); m = \frac{5}{6}$       25.  $(0, y), (-2, 1); m = -8$       26.  $(8, 1), (x, 7); m = -\frac{1}{2}$   
 27.  $(5, 4), (-5, y); m = \frac{3}{5}$       28.  $(-9, y), (0, -3); m = -\frac{7}{9}$       29.  $(x, 9), (-1, 19); m = 5$   
 30.  $(9, 3), (-6, 7y); m = 3$       31.  $(-3, y + 1), (0, 4); m = 6$       32.  $(\frac{x}{2}, 7), (-10, 15); m = 4$

33. **REASONING** The point  $(-1, 8)$  is on a line that has a slope of  $-3$ . Is the point  $(4, -7)$  on the same line? *Explain* your reasoning.
34. **★ WRITING** Is a line with undefined slope the graph of a function? *Explain*.
35. **CHALLENGE** Given two points  $(x_1, y_1)$  and  $(x_2, y_2)$  such that  $x_1 \neq x_2$ , show that  $\frac{y_2 - y_1}{x_2 - x_1} = \frac{y_1 - y_2}{x_1 - x_2}$ . What does this result tell you about calculating the slope of a line?

## PROBLEM SOLVING

**EXAMPLE 6**  
on p. 238  
for Exs. 36–37

36. **OCEANOGRAPHY** Ocean water levels are measured hourly at a monitoring station. The table shows the water level (in meters) on one particular morning. *Describe* the rates of change in water levels throughout the morning.

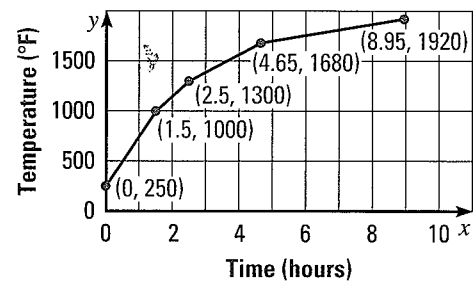
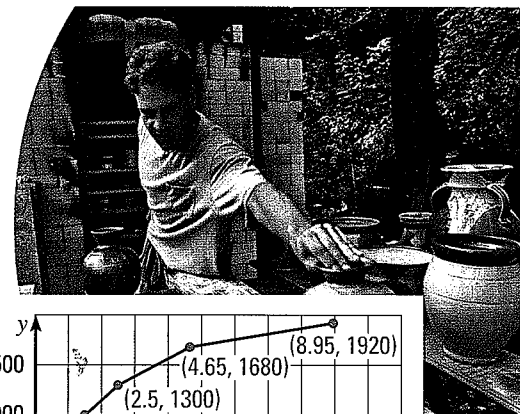
Hours since 12:00 A.M.	1	3	8	10	12
Water level (meters)	2	1.4	0.5	1	1.8

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37. **MULTI-STEP PROBLEM** Firing a piece of pottery in a kiln takes place at different temperatures for different amounts of time. The graph shows the temperatures in a kiln while firing a piece of pottery (after the kiln is preheated to  $250^\circ\text{F}$ ).

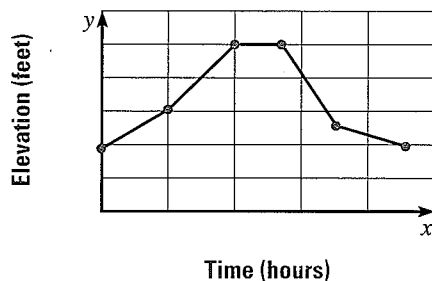
- Determine the time interval during which the temperature in the kiln showed the greatest rate of change.
- Determine the time interval during which the temperature in the kiln showed the least rate of change.

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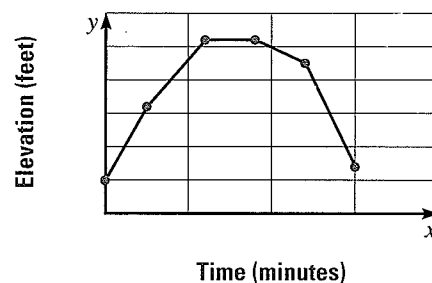


**EXAMPLE 7**  
on p. 238  
for Exs. 38–39

38. **FLYING** The graph shows the altitude of a plane during 4 hours of a flight. Give a verbal description of the flight.

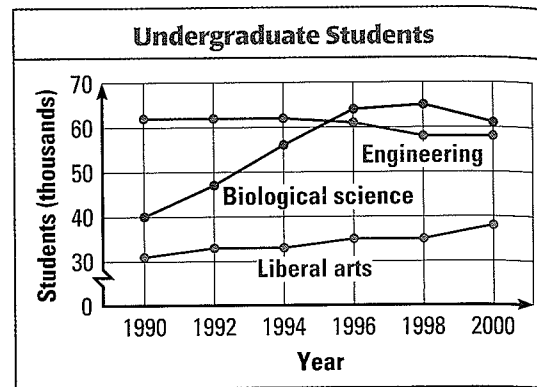


39. **HIKING** The graph shows the elevation of a hiker walking on a mountain trail. Give a verbal description of the hike.

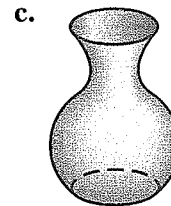
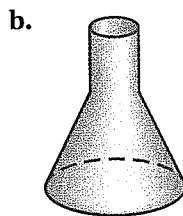
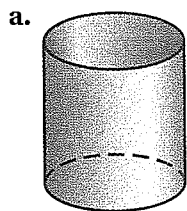


40. ★ **EXTENDED RESPONSE** The graph shows the number (in thousands) of undergraduate students who majored in biological science, engineering, or liberal arts in the United States from 1990 to 2000.

- During which two-year period did the number of engineering students decrease the most? Estimate the rate of change for this time period.
- During which two-year period did the number of liberal arts students increase the most? Estimate the rate of change for this time period.
- How did the total number of students majoring in biological science, engineering, and liberal arts change in the 10 year period? *Explain* your thinking.



41. **CHALLENGE** Imagine the containers below being filled with water at a constant rate. Sketch a graph that shows the water level for each container during the time it takes to fill the container with water.



## MIXED REVIEW

Check whether the given number is a solution of the equation or inequality. (p. 21)

42.  $4b - 7 = b + 11$ ; 6

43.  $x - 8 = -2x - 14$ ; -1

44.  $\frac{t}{4} + 9 = 13$ ; 16

45.  $a + 9 > 20$ ; 3

46.  $\frac{y+3}{2} < 13$ ; 23

47.  $2(p+5) \leq 75$ ; 4

Evaluate the expression. Approximate the square root to the nearest integer, if necessary. (p. 110)

48.  $\sqrt{16}$

49.  $-\sqrt{9}$

50.  $\pm\sqrt{45}$

51.  $\sqrt{136}$

52.  $\pm\sqrt{64}$

53.  $-\sqrt{33}$

54.  $\pm\sqrt{154}$

55.  $\pm\sqrt{256}$

56.  $\sqrt{4761}$

### PREVIEW

Prepare for  
Lesson 4.5 in  
Exs. 57–62.

Find the  $x$ -intercept and the  $y$ -intercept of the graph of the equation. (p. 225)

57.  $y = x + 7$

58.  $y = -x - 1$

59.  $y = 8 - 2x$

60.  $y = 3x + 5$

61.  $y = 4x - 10$

62.  $y = -9 + 6x$



## 4.5 Slope and y-Intercept

**QUESTION** How can you use the equation of a line to find its slope and y-intercept?

**EXPLORE** Find the slopes and the y-intercepts of lines

**STEP 1** Find  $y$  when  $x = 0$

Copy the table below. Let  $x_1 = 0$  and find  $y_1$  for each equation. Use your answers to complete the second and fifth columns in the table.

**STEP 2** Find  $y$  when  $x = 2$

Let  $x_2 = 2$  and find  $y_2$  for each equation. Use your answers to complete the third column in the table.

**STEP 3** Compute the slope

Use the slope formula and the ordered pairs you found in the second and third columns to complete the fourth column.

Line	$(0, y_1)$	$(2, y_2)$	Slope	y-intercept
$y = 4x + 3$	$(0, 3)$	$(2, 11)$	$\frac{11 - 3}{2 - 0} = 4$	3
$y = -2x + 3$	$(0, ?)$	$(2, ?)$	?	?
$y = \frac{1}{2}x + 4$	$(0, ?)$	$(2, ?)$	?	?
$y = -4x - 3$	$(0, ?)$	$(2, ?)$	?	?
$y = -\frac{1}{4}x - 3$	$(0, ?)$	$(2, ?)$	?	?

**DRAW CONCLUSIONS** Use your observations to complete these exercises

- Compare the slope of each line with the equation of the line. What do you notice?
- Compare the y-intercept of each line with the equation of the line. What do you notice?

**Predict the slope and the y-intercept of the line with the given equation. Then check your predictions by finding the slope and y-intercept as you did in the table above.**

3.  $y = -5x + 1$

4.  $y = \frac{3}{4}x + 2$

5.  $y = -\frac{3}{2}x - 1$

6. **REASONING** Use the procedure you followed to complete the table above to show that the y-intercept of the graph of  $y = mx + b$  is  $b$  and the slope of the graph is  $m$ .

# 4.5 EXERCISES

**HOMWORK KEY**

○ = WORKED-OUT SOLUTIONS  
on p. WS9 for Exs. 11, 21, and 41

★ = STANDARDIZED TEST PRACTICE  
Exs. 2, 9, 10, 36, 42, and 44

## SKILL PRACTICE

1. **VOCABULARY** Copy and complete: Two lines in the same plane are   ?   if they do not intersect.

2. ★ **WRITING** What is the slope-intercept form of a linear equation? Explain why this form is called slope-intercept form.

**EXAMPLE 1**  
on p. 244  
for Exs. 3–16

**SLOPE AND y-INTERCEPT** Identify the slope and y-intercept of the line with the given equation.

3.  $y = 2x + 1$

4.  $y = -x$

5.  $y = 6 - 3x$

6.  $y = -7 + 5x$

7.  $y = \frac{2}{3}x - 1$

8.  $y = -\frac{1}{4}x + 8$

9. ★ **MULTIPLE CHOICE** What is the slope of the line with the equation  $y = -18x - 9$ ?

(A) -18

(B) -9

(C) 9

(D) 18

10. ★ **MULTIPLE CHOICE** What is the y-intercept of the line with the equation  $x - 3y = -12$ ?

(A) -12

(B) -4

(C) 4

(D) 12

**REWRITING EQUATIONS** Rewrite the equation in slope-intercept form. Then identify the slope and the y-intercept of the line.

11.  $4x + y = 1$

12.  $x - y = 6$

13.  $6x - 3y = -9$

14.  $-12x - 4y = 2$

15.  $2x + 5y = -10$

16.  $-x - 10y = 20$

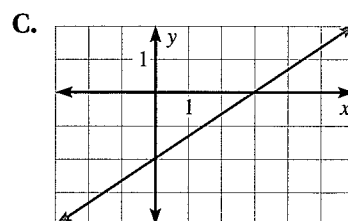
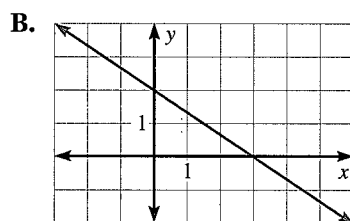
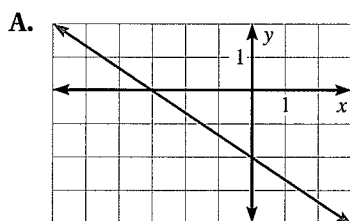
**EXAMPLE 2**  
on p. 245  
for Exs. 17–29

**MATCHING EQUATIONS WITH GRAPHS** Match the equation with its graph.

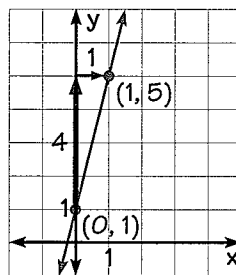
17.  $2x + 3y = 6$

18.  $2x + 3y = -6$

19.  $2x - 3y = 6$



20. **ERROR ANALYSIS** Describe and correct the error in graphing the equation  $y = 4x - 1$ .



**GRAPHING EQUATIONS** Graph the equation.

21.  $y = -6x + 1$

22.  $y = 3x + 2$

23.  $y = -x + 7$

24.  $y = \frac{2}{3}x$

25.  $y = \frac{1}{4}x - 5$

26.  $y = -\frac{5}{2}x + 2$

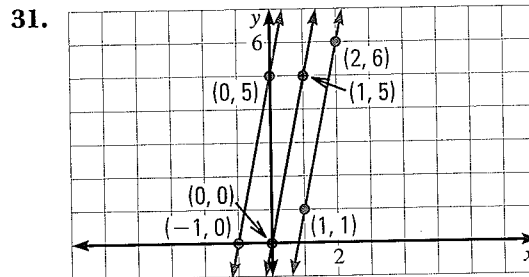
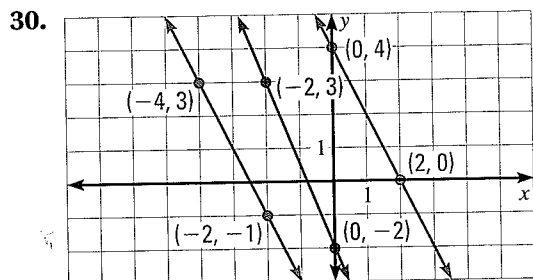
27.  $7x - 2y = -11$

28.  $-8x - 2y = 32$

29.  $-x - 0.5y = 2.5$

**EXAMPLE 5**  
on p. 246  
for Exs. 30–35

**PARALLEL LINES** Determine which lines are parallel.



**PARALLEL LINES** Tell whether the graphs of the two equations are parallel lines. *Explain your reasoning.*

32.  $y = 5x - 7, 5x + y = 7$

33.  $y = 3x + 2, -7 + 3x = y$

34.  $y = -0.5x, x + 2y = 18$

35.  $4x + y = 3, x + 4y = 3$

36. **★ OPEN-ENDED** Write the equation of a line that is parallel to  $6x + y = 24$ . *Explain your reasoning.*

**REASONING** Find the value of  $k$  so that the lines through the given points are parallel.

37. Line 1:  $(-4, -2)$  and  $(0, 0)$   
Line 2:  $(2, 7)$  and  $(k, 5)$

38. Line 1:  $(-1, 9)$  and  $(-6, -6)$   
Line 2:  $(-7, k)$  and  $(0, -2)$

39. **CHALLENGE** Find the slope and  $y$ -intercept of the graph of the equation  $Ax + By = C$  where  $B \neq 0$ . Use your results to find the slope and  $y$ -intercept of the graph of  $3x + 2y = 18$ .

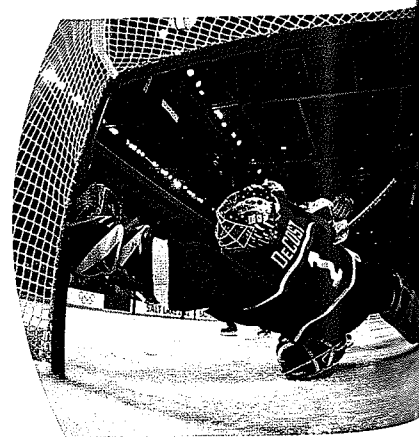
**PROBLEM SOLVING**

**EXAMPLES 3 and 4**  
on pp. 245–246  
for Exs. 40–44

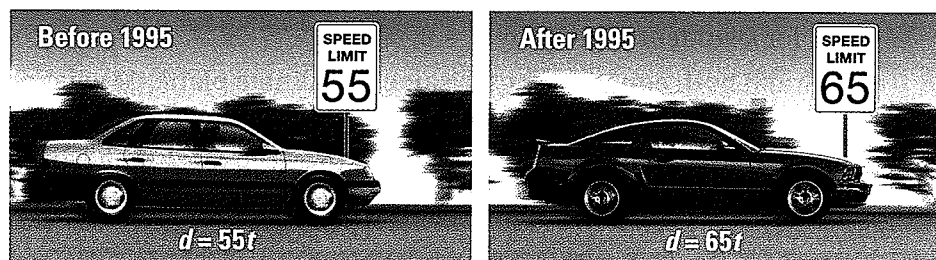
40. **HOCKEY** Your family spends \$60 on tickets to a hockey game and \$4 per hour for parking. The total cost  $C$  (in dollars) is given by  $C = 60 + 4t$  where  $t$  is the time (in hours) your family's car is parked.

- Graph the equation.
- Suppose the parking fee is raised to \$5.50 per hour so that the total cost of tickets and parking for  $t$  hours is  $C = 60 + 5.5t$ . Graph the equation in the same coordinate plane as the equation in part (a).
- How much more does it cost to go to a game for 4 hours after the parking fee is raised?

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41. **SPEED LIMITS** In 1995 Pennsylvania changed its maximum speed limit on rural interstate highways, as shown below. The diagram also shows the distance  $d$  (in miles) a person could travel driving at the maximum speed limit for  $t$  hours both before and after 1995.



- Graph both equations in the same coordinate plane.
- Use the graphs to find the difference of the distances a person could drive in 3 hours before and after the speed limit was changed.

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42. **★ SHORT RESPONSE** A service station charges \$40 per hour for labor plus the cost of parts to repair a car. Parts can either be ordered from the car dealership for \$250 or from a warehouse for \$200. The equations below give the total repair cost  $C$  (in dollars) for a repair that takes  $t$  hours using parts from the dealership or from the warehouse.

**Dealership:**  $C = 40t + 250$       **Warehouse:**  $C = 40t + 200$

- Graph both equations in the same coordinate plane.
  - Use the graphs to find the difference of the costs if the repair takes 3 hours. What if the repair takes 4 hours? What do you notice about the differences of the costs? *Explain.*
43. **FACTORY SHIFTS** Welders at a factory can work one of two shifts. Welders on the first shift earn \$12 per hour while workers on the second shift earn \$14 per hour. The total amount  $a$  (in dollars) a first-shift worker earns is given by  $a = 12t$  where  $t$  is the time (in hours) worked. The total amount a second-shift worker earns is given by  $a = 14t$ .
- Graph both equations in the same coordinate plane. What do the slopes and the  $a$ -intercepts of the graphs mean in this situation?
  - How much more money does a welder earn for a 40 hour week if he or she works the second shift rather than the first shift?
44. **★ EXTENDED RESPONSE** An artist is renting a booth at an art show. A small booth costs \$350 to rent. The artist plans to sell framed pictures for \$50 each. The profit  $P$  (in dollars) the artist makes after selling  $p$  pictures is given by  $P = 50p - 350$ .
- Graph the equation.
  - If the artist decides to rent a larger booth for \$500, the profit is given by  $P = 50p - 500$ . Graph this equation on the same coordinate plane you used in part (a).
  - The artist can display 80 pictures in the small booth and 120 in the larger booth. If the artist is able to sell all of the pictures, which booth should the artist rent? *Explain.*

45. **CHALLENGE** To use a rock climbing wall at a college, a person who does not attend the college has to pay a \$5 certification fee plus \$3 per visit. The total cost  $C$  (in dollars) for a person who does not attend the college is given by  $C = 3v + 5$  where  $v$  is the number of visits to the rock climbing wall. A student at the college pays only an \$8 certification fee, so the total cost for a student is given by  $C = 8$ .

- Graph both equations in the same coordinate plane. At what point do the lines intersect? What does the point of intersection represent?
- When will a nonstudent pay more than a student? When will a student pay more than a nonstudent? *Explain.*

## MIXED REVIEW

Simplify the expression. (p. 96)

46.  $3(x + 24)$

47.  $5(x - 5)$

48.  $8(x - 6)$

Solve the equation.

49.  $3x + x = 8$  (p. 141)

50.  $5(x - 3x) = 15$  (p. 148)

51.  $\frac{4}{3}(8x - 3) = 16$  (p. 148)

Find the slope of the line that passes through the points. (p. 235)

52. (3, 4) and (9, 5)

53. (4, -4) and (-2, 2)

54. (-3, -7) and (0, -7)

Solve the proportion. Check your solution. (p. 168)

55.  $\frac{4}{5} = \frac{x}{50}$

56.  $\frac{2x}{x+4} = \frac{8}{9}$

57.  $\frac{7t-2}{8} = \frac{3t-4}{5}$

**PREVIEW**  
Prepare for  
Lesson 4.6  
in Exs. 52–57.

## QUIZ for Lessons 4.4–4.5

Find the slope of the line that passes through the points. (p. 235)

1. (3, -11) and (0, 4)

2. (2, 1) and (8, 4)

3. (-4, -1) and (-1, -1)

Identify the slope and  $y$ -intercept of the line with the given equation. (p. 244)

4.  $y = -x + 9$

5.  $2x + 9y = -18$

6.  $-x + 6y = 21$

Graph the equation. (p. 244)

7.  $y = -2x + 11$

8.  $y = \frac{5}{3}x - 8$

9.  $-3x - 4y = -12$

10. **RED OAKS** Red oak trees grow at a rate of about 2 feet per year. You buy and plant two red oak trees, one that is 6 feet tall and one that is 8 feet tall. The height  $h$  (in feet) of the shorter tree can be modeled by  $h = 2t + 6$  where  $t$  is the time (in years) since you planted the tree. The height of the taller tree can be modeled by  $h = 2t + 8$ . (p. 244)

- Graph both equations in the same coordinate plane.
- Use the graphs to find the difference of the heights of the trees 5 years after you plant them. What is the difference after 10 years? What do you notice about the difference of the heights of the two trees?

## Extension

Use after Lesson 4.5

# Solve Linear Equations by Graphing

**GOAL** Use graphs to solve linear equations.

In Chapter 3, you learned how to solve linear equations in one variable algebraically. You can also solve linear equations graphically.

### KEY CONCEPT

*For Your Notebook*

#### Steps for Solving Linear Equations Graphically

Use the following steps to solve a linear equation in one variable graphically.

**STEP 1** Write the equation in the form  $ax + b = 0$ .

**STEP 2** Write the related function  $y = ax + b$ .

**STEP 3** Graph the equation  $y = ax + b$ .

The solution of  $ax + b = 0$  is the  $x$ -intercept of the graph of  $y = ax + b$ .

### EXAMPLE 1 Solve an equation graphically

Solve  $\frac{5}{2}x + 2 = 3x$  graphically. Check your solution algebraically.

#### Solution

**STEP 1** Write the equation in the form  $ax + b = 0$ .

$$\frac{5}{2}x + 2 = 3x \quad \text{Write original equation.}$$

$$-\frac{1}{2}x + 2 = 0 \quad \text{Subtract } 3x \text{ from each side.}$$

**STEP 2** Write the related function  $y = -\frac{1}{2}x + 2$ .

**STEP 3** Graph the equation  $y = -\frac{1}{2}x + 2$ . The  $x$ -intercept is 4.

► The solution of  $\frac{5}{2}x + 2 = 3x$  is 4.

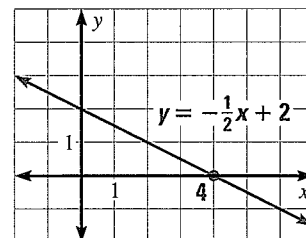
**CHECK** Use substitution.

$$\frac{5}{2}x + 2 = 3x \quad \text{Write original equation.}$$

$$\frac{5}{2}(4) + 2 \stackrel{?}{=} 3(4) \quad \text{Substitute 4 for } x.$$

$$10 + 2 = 12 \quad \text{Simplify.}$$

$$12 = 12 \checkmark \quad \text{Solution checks.}$$





## EXAMPLE 2 Approximate a real-world solution

**POPULATION** The United States population  $P$  (in millions) can be modeled by the function  $P = 2.683t + 213.1$  where  $t$  is the number of years since 1975. In approximately what year will the population be 350 million?

### Solution

Substitute 350 for  $P$  in the linear model. You can answer the question by solving the resulting linear equation  $350 = 2.683t + 213.1$ .

**STEP 1** Write the equation in the form  $ax + b = 0$ .

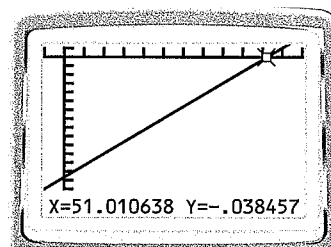
$$350 = 2.683t + 213.1 \quad \text{Write equation.}$$

$$0 = 2.683t - 136.9 \quad \text{Subtract 350 from each side.}$$

$$0 = 2.683x - 136.9 \quad \text{Substitute } x \text{ for } t.$$

**STEP 2** Write the related function:  $y = 2.683x - 136.9$ .

**STEP 3** Graph the related function on a graphing calculator. Use the *trace* feature to approximate the  $x$ -intercept. You will know that you've crossed the  $x$ -axis when the  $y$ -values change from negative to positive. The  $x$ -intercept is about 51.



► Because  $x$  is the number of years since 1975, you can estimate that the population will be 350 million about 51 years after 1975, or in 2026.

### SET THE WINDOW

Use the following viewing window for Example 2.

Xmin=-5  
Xmax=60  
Xscl=5  
Ymin=-150  
Ymax=10  
Yscl=10

## PRACTICE

### EXAMPLE 1

on p. 251  
for Exs. 1-6

Solve the equation graphically. Then check your solution algebraically.

1.  $6x + 5 = -7$

2.  $-7x + 18 = -3$

3.  $2x - 4 = 3x$

4.  $\frac{1}{2}x - 3 = 2x$

5.  $-4 + 9x = -3x + 2$

6.  $10x - 18x = 4x - 6$

### EXAMPLE 2

on p. 252  
for Exs. 7-9

7. **CABLE TELEVISION** The number  $s$  (in millions) of cable television subscribers can be modeled by the function  $s = 1.79t + 51.1$  where  $t$  is the number of years since 1990. Use a graphing calculator to approximate the year when the number of subscribers was 70 million.

8. **EDUCATION** The number  $b$  (in thousands) of bachelor's degrees in Spanish earned in the U.S. can be modeled by the function  $b = 0.281t + 4.26$  where  $t$  is the number of years since 1990. Use a graphing calculator to approximate the year when the number of degrees will be 9000.

9. **TRAVEL** The number of miles  $m$  (in billions) traveled by vehicles in New York can be modeled by  $m = 2.56t + 113$  where  $t$  is the number of years since 1994. Use a graphing calculator to approximate the year in which the number of vehicle miles of travel in New York was 130 billion.

**RATIOS** The direct variation equation  $y = ax$  can be rewritten as  $\frac{y}{x} = a$  for  $x \neq 0$ . So, in a direct variation, the ratio of  $y$  to  $x$  is constant for all nonzero data pairs  $(x, y)$ .

### EXAMPLE 5 Use a direct variation model

**ONLINE MUSIC** The table shows the cost  $C$  of downloading  $s$  songs at an Internet music site.

Number of songs, $s$	Cost, $C$ (dollars)
3	2.97
5	4.95
7	6.93

- Explain why  $C$  varies directly with  $s$ .
- Write a direct variation equation that relates  $s$  and  $C$ .

#### Solution

- To explain why  $C$  varies directly with  $s$ , compare the ratios  $\frac{C}{s}$  for all data pairs  $(s, C)$ :  $\frac{2.97}{3} = \frac{4.95}{5} = \frac{6.93}{7} = 0.99$ .  
Because the ratios all equal 0.99,  $C$  varies directly with  $s$ .
- A direct variation equation is  $C = 0.99s$ .

#### CHECK RATIOS

For real-world data, the ratios may not be exactly equal. You may still be able to use a direct variation model when the ratios are approximately equal.



#### GUIDED PRACTICE for Example 5

- WHAT IF?** In Example 5, suppose the website charges a total of \$1.99 for the first 5 songs you download and \$.99 for each song after the first 5. Is it reasonable to use a direct variation model for this situation? *Explain.*

## 4.6 EXERCISES

#### HOMEWORK KEY

- = WORKED-OUT SOLUTIONS on p. WS9 for Exs. 7, 21, and 43
- ★ = STANDARDIZED TEST PRACTICE Exs. 2, 9, 28, 38, 43, 44, and 46
- ◆ = MULTIPLE REPRESENTATIONS Ex. 45

### SKILL PRACTICE

- VOCABULARY** Copy and complete: Two variables  $x$  and  $y$  show   ? provided  $y = ax$  and  $a \neq 0$ .
- ★ **WRITING** A line has a slope of  $-3$  and a  $y$ -intercept of 4. Is the equation of the line a direct variation equation? *Explain.*

#### EXAMPLE 1

on p. 253  
for Exs. 3–10

**IDENTIFYING DIRECT VARIATION EQUATIONS** Tell whether the equation represents direct variation. If so, identify the constant of variation.

3.  $y = x$

4.  $y = 5x - 1$

5.  $2x + y = 3$

6.  $x - 3y = 0$

7.  $8x + 2y = 0$

8.  $2.4x + 6 = 1.2y$

9. ★ **MULTIPLE CHOICE** Which equation is a direct variation equation?

- (A)  $y = 7 - 3x$     (B)  $3x - 7y = 1$     (C)  $3x - 7y = 0$     (D)  $3y = 7x - 1$

10. **ERROR ANALYSIS** Describe and correct the error in identifying the constant of variation for the direct variation equation  $-5x + 3y = 0$ .

$$\begin{aligned} -5x + 3y &= 0 \\ 3y &= 5x \end{aligned}$$

The constant of variation is 5.



**EXAMPLE 2**

on p. 254  
for Exs. 11–22

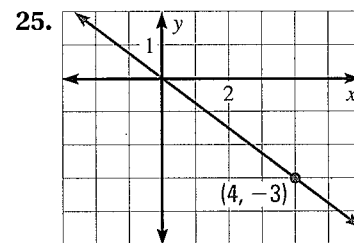
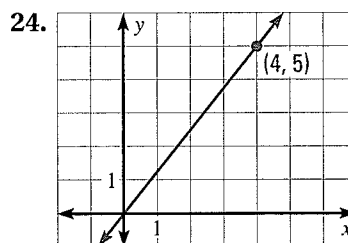
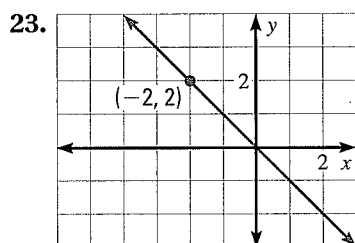
**GRAPHING EQUATIONS** Graph the direct variation equation.

11.  $y = x$     12.  $y = 3x$     13.  $y = -4x$     14.  $y = 5x$   
 15.  $y = \frac{4}{3}x$     16.  $y = \frac{1}{2}x$     17.  $y = -\frac{1}{3}x$     18.  $y = -\frac{3}{2}x$   
 19.  $12y = -24x$     20.  $10y = 25x$     (21)  $4x + y = 0$     22.  $y - 1.25x = 0$

**EXAMPLE 3**

on p. 254  
for Exs. 23–25

**WRITING EQUATIONS** The graph of a direct variation equation is shown. Write the direct variation equation. Then find the value of  $y$  when  $x = 8$ .



**IDENTIFYING DIRECT VARIATION EQUATIONS** Tell whether the table represents direct variation. If so, write the direct variation equation.

26. 

$x$	1	2	3	4	6
$y$	5	10	15	20	30

27. 

$x$	-3	-1	1	3	5
$y$	-2	0	2	4	6

28. ★ **WRITING** A student says that a direct variation equation can be used to model the data in the table. Explain why the student is mistaken.

$x$	2	4	8	16
$y$	1	2	4	6

**WRITING EQUATIONS** Given that  $y$  varies directly with  $x$ , use the specified values to write a direct variation equation that relates  $x$  and  $y$ .

29.  $x = 3, y = 9$     30.  $x = 2, y = 26$     31.  $x = 14, y = 7$   
 32.  $x = 15, y = -5$     33.  $x = -2, y = -2$     34.  $x = -18, y = -4$   
 35.  $x = \frac{1}{4}, y = 1$     36.  $x = -6, y = 15$     37.  $x = -5.2, y = 1.4$

38. ★ **WRITING** If  $y$  varies directly with  $x$ , does  $x$  vary directly with  $y$ ? If so, what is the relationship between the constants of variation? Explain.

39. **CHALLENGE** The slope of a line is  $-\frac{1}{3}$ , and the point  $(-6, 2)$  lies on the line.

Use the formula for the slope of a line to determine if the equation of the line is a direct variation equation.

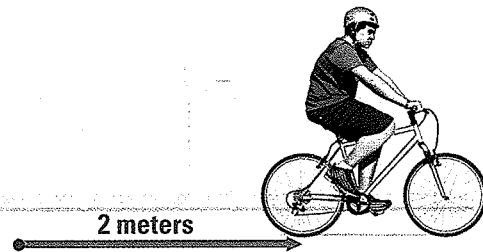
## PROBLEM SOLVING

**EXAMPLE 4**  
on p. 255  
for Exs. 40–42

- 40. BICYCLES** The distance  $d$  (in meters) you travel on a bicycle varies directly with the number  $r$  of revolutions that the rear tire completes. You travel about 2 meters on a mountain bike for every revolution of the tire.



1 revolution



2 meters

- a. Write a direct variation equation that relates  $r$  and  $d$ .
- b. How many meters do you travel in 1500 tire revolutions?

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- 41. VACATION TIME** At one company, the amount of vacation  $v$  (in hours) an employee earns varies directly with the amount of time  $t$  (in weeks) he or she works. An employee who works 2 weeks earns 3 hours of vacation.

- a. Write a direct variation equation that relates  $t$  and  $v$ .
- b. How many hours of vacation time does an employee earn in 8 weeks?

**@HomeTutor** for problem solving help at classzone.com

- 42. LANDSCAPING** Landscapers plan to spread a layer of stone on a path. The number  $s$  of bags of stone needed depends on the depth  $d$  (in inches) of the layer. They need 10 bags to spread a layer of stone that is 2 inches deep. Write a direct variation equation that relates  $d$  and  $s$ . Then find the number of bags needed to spread a layer that is 3 inches deep.

**EXAMPLE 5**  
on p. 256  
for Exs. 43–44

- 43. ★ SHORT RESPONSE** At a recycling center, computers and computer accessories can be recycled for a fee  $f$  based on weight  $w$ , as shown in the table.

Weight, $w$ (pounds)	Fee, $f$ (dollars)
10	2.50
15	3.75
30	7.50

- a. Explain why  $f$  varies directly with  $w$ .
- b. Write a direct variation equation that relates  $w$  and  $f$ . Find the total recycling fee for a computer that weighs 18 pounds and a printer that weighs 10 pounds.

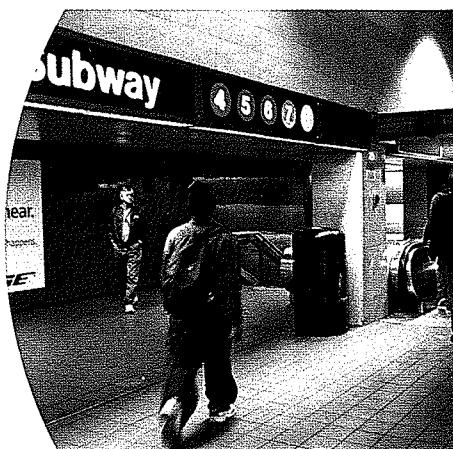
- 44. ★ SHORT RESPONSE** You can buy gold chain by the inch. The table shows the price of gold chain for various lengths.

Length, $l$ (inches)	7	9	16	18
Price, $p$ (dollars)	8.75	11.25	20.00	22.50

- a. Explain why  $p$  varies directly with  $l$ .
- b. Write a direct variation equation that relates  $l$  and  $p$ . If you have \$30, what is the longest chain that you can buy?

45. **MULTIPLE REPRESENTATIONS** The total cost of riding the subway to and from school every day is \$1.50.

- a. **Making a Table** Make a table that shows the number  $d$  of school days and the total cost  $C$  (in dollars) for trips to and from school for some values of  $d$ . Assume you travel to school once each school day and home from school once each school day.
- b. **Drawing a Graph** Graph the ordered pairs from the table and draw a ray through them.
- c. **Writing an Equation** Write an equation of the graph from part (b). Is it a direct variation equation? *Explain.* If there are 22 school days in one month, what will it cost to ride the subway to and from school for that month?



46. **★ EXTENDED RESPONSE** The table shows the average number of field goals attempted  $t$  and the average number of field goals made  $m$  per game for all NCAA Division I women's basketball teams for 9 consecutive seasons.

Attempted field goals, $t$	61.8	61.9	61.8	60.8	59.5	59.0	58.9	59.2	58.4
Field goals made, $m$	25.7	25.6	25.6	25.2	24.5	24.6	24.5	24.3	24.0

- a. **Write** Why is it reasonable to use a direct variation model for this situation? Write a direct variation equation that relates  $t$  and  $m$ . Find the constant of variation to the nearest tenth.
- b. **Estimate** The highest average number of attempted field goals in one season was 66.2. Estimate the number of field goals made that season.
- c. **Explain** If the average number of field goals made was increasing rather than decreasing and the number of attempted field goals continued to decrease, would the data show direct variation? *Explain.*
47. **CHALLENGE** In Exercise 40, you found an equation showing that the distance traveled on a bike varies directly with the number of revolutions that the rear tire completes. The number  $r$  of tire revolutions varies directly with the number  $p$  of pedal revolutions. In a particular gear, you travel about 1.3 meters for every 5 revolutions of the pedals. Show that distance traveled varies directly with pedal revolutions.

## MIXED REVIEW

Graph the equation.

48.  $y = -8$  (p. 215)

49.  $x = 6$  (p. 215)

50.  $2x + y = 4$  (p. 225)

51.  $-2x + 5y = -30$  (p. 225)

52.  $0.4x + 2y = 6$  (p. 225)

53.  $y = 2x - 5$  (p. 244)

54.  $y = \frac{1}{3}x$  (p. 244)

55.  $y = -x + 3$  (p. 244)

56.  $y = -\frac{3}{2}x + 2$  (p. 244)

Identify the slope and  $y$ -intercept of the line with the given equation. (p. 244)

57.  $y = 3x + 5$

58.  $y = -3x$

59.  $y = 2x - 5$

60.  $y = 4x - 11$

61.  $y = \frac{4}{5}x - 3$

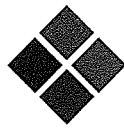
62.  $y = \frac{5}{4}x + 3.1$

### PREVIEW

Prepare for  
Lesson 4.7  
in Exs. 57–62.



**Another Way to Solve Example 4, page 255**



**MULTIPLE REPRESENTATIONS** In Example 4 on page 255, you saw how to solve the problem about how much salt to add to a saltwater fish tank by writing and using a direct variation equation. You can also solve the problem using a graph or a proportion.

**PROBLEM**

**SALTWATER AQUARIUM** The number  $s$  of tablespoons of sea salt needed in a saltwater fish tank varies directly with the number  $w$  of gallons of water in the tank. A pet shop owner recommends adding 100 tablespoons of sea salt to a 20 gallon tank. How many tablespoons of salt should be added to a 30 gallon saltwater fish tank?

**METHOD 1**

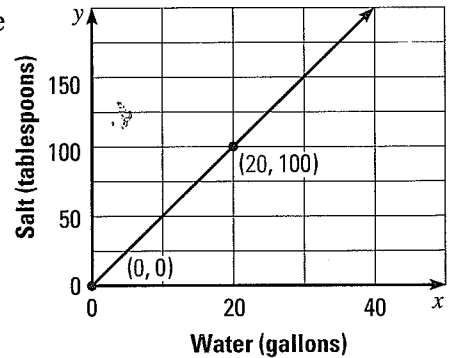
**Using a Graph** An alternative approach is to use a graph.

**STEP 1** Read the problem. It tells you an amount of salt for a certain size fish tank. You can also assume that if a fish tank has no water, then no salt needs to be added. Write ordered pairs for this information.

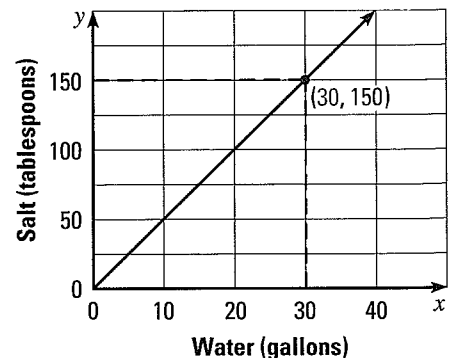
Number of gallons	Tablespoons of salt
(20, 100)	
(0, 0)	

**STEP 2** Graph the ordered pairs. Draw a line through the points.

The coordinates of points on the line give the amounts of salt that should be added to fish tanks of various sizes.



**STEP 3** Find the point on the graph that has an  $x$ -coordinate of 30. The  $y$ -coordinate of this point is 150, so 150 tablespoons of salt should be added to a 30 gallon tank.





**METHOD 2**

**Writing a Proportion** Another alternative approach is to write and solve a proportion.

**STEP 1** Write a proportion involving two ratios that each compare the amount of water (in gallons) to the amount of salt (in tablespoons).

$$\frac{20}{100} = \frac{30}{s}$$

← amount of water (gallons)  
← amount of salt (tablespoons)

**STEP 2** Solve the proportion.

$$\frac{20}{100} = \frac{30}{s} \quad \text{Write proportion.}$$

$$20s = 100 \cdot 30 \quad \text{Cross products property}$$

$$20s = 3000 \quad \text{Simplify.}$$

$$s = 150 \quad \text{Divide each side by 20.}$$

► You should add 150 tablespoons of salt to a 30 gallon tank.

**CHECK** Check your answer by writing each ratio in simplest form.

$$\frac{20}{100} = \frac{1}{5} \text{ and } \frac{30}{150} = \frac{1}{5}$$

Because each ratio simplifies to  $\frac{1}{5}$ , the answer is correct.

**PRACTICE**

- WHAT IF?** Suppose the fish tank in the problem above is a 22 gallon tank. How many tablespoons of salt should be added to the tank? *Describe* which method you used to solve this problem.
- ADVERTISING** A local newspaper charges by the word for printing classified ads. A 14 word ad costs \$5.88. How much would a 21 word ad cost? Solve this problem using two different methods.
- REASONING** In Exercise 2, how can you quickly determine the cost of a 7 word ad? *Explain* how you could use the cost of a 7 word ad to solve the problem.
- NUTRITION** A company sells fruit smoothies in two sizes of bottles: 6 fluid ounces and 10 fluid ounces. You know that a 6 ounce bottle contains 96 milligrams of sodium. How many milligrams of sodium does a 10 ounce bottle contain?
- ERROR ANALYSIS** A student solved the problem in Exercise 4 as shown. *Describe* and correct the error made.
 

Let  $x$  = the number of milligrams of sodium in a 10 ounce bottle.

$$\frac{6}{x} = \frac{10}{96}$$

$$576 = 10x$$

$$57.6 = x$$
- SLEEPING** You find an online calculator that calculates the number of calories you burn while sleeping. The results for various sleeping times are shown. About how many more calories would you burn by sleeping for 9.5 hours than for 8 hours? Choose any method for solving the problem.

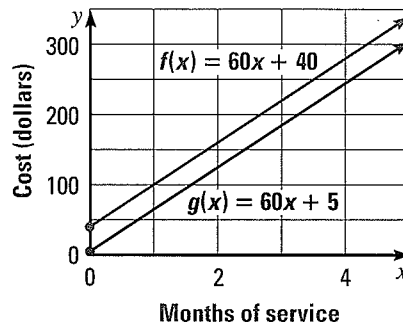
<b>Hours of sleep</b>	6.5	7	8.5	9
<b>Calories burned</b>	390	420	510	540

## EXAMPLE 5 Graph real-world functions

**CABLE** A cable company charges new customers \$40 for installation and \$60 per month for its service. The cost to the customer is given by the function  $f(x) = 60x + 40$  where  $x$  is the number of months of service. To attract new customers, the cable company reduces the installation fee to \$5. A function for the cost with the reduced installation fee is  $g(x) = 60x + 5$ . Graph both functions. How is the graph of  $g$  related to the graph of  $f$ ?

### Solution

The graphs of both functions are shown. Both functions have a slope of 60, so they are parallel. The  $y$ -intercept of the graph of  $g$  is 35 less than the graph of  $f$ . So, the graph of  $g$  is a vertical translation of the graph of  $f$ .



### REVIEW TRANSFORMATIONS

For help with transformations, see pp. 922–923.

### GUIDED PRACTICE for Example 5

4. **WHAT IF?** In Example 5, suppose the monthly fee is \$70 so that the cost to the customer is given by  $h(x) = 70x + 40$ . Graph  $f$  and  $h$  in the same coordinate plane. How is the graph of  $h$  related to the graph of  $f$ ?

## 4.7 EXERCISES

### HOMEWORK KEY

- = WORKED-OUT SOLUTIONS on p. WS10 for Exs. 3, 17, and 39  
★ = STANDARDIZED TEST PRACTICE Exs. 2, 13, 22, 35, 36, 44, and 45

### SKILL PRACTICE

1. **VOCABULARY** When you write the function  $y = 3x + 12$  as  $f(x) = 3x + 12$ , you are using   ?  .
2. ★ **WRITING** Would the functions  $f(x) = -9x + 12$ ,  $g(x) = -9x - 2$ , and  $h(x) = -9x$  be considered a family of functions? *Explain.*

**EVALUATING FUNCTIONS** Evaluate the function when  $x = -2, 0$ , and  $3$ .

- |                              |                                |                               |
|------------------------------|--------------------------------|-------------------------------|
| 3. $f(x) = 12x + 1$          | 4. $g(x) = -3x + 5$            | 5. $p(x) = -8x - 2$           |
| 6. $h(x) = 2.25x$            | 7. $m(x) = -6.5x$              | 8. $f(x) = -0.75x - 1$        |
| 9. $s(x) = \frac{2}{5}x + 3$ | 10. $d(x) = -\frac{3}{2}x + 5$ | 11. $h(x) = \frac{3}{4}x - 6$ |

12. **ERROR ANALYSIS** Describe and correct the error in evaluating the function  $g(x) = -5x + 3$  when  $x = -3$ .

$$\begin{aligned} g(-3) &= -5(-3) + 3 \\ -3g &= 18 \\ g &= -6 \end{aligned}$$

**EXAMPLE 1**  
on p. 262  
for Exs. 3–13

13. ★ **MULTIPLE CHOICE** Given  $f(x) = -6.8x + 5$ , what is the value of  $f(-2)$ ?

- (A) -18.6      (B) -8.6      (C) 8.6      (D) 18.6

**EXAMPLE 2**

on p. 262  
for Exs. 14–22

**FINDING X-VALUES** Find the value of  $x$  so that the function has the given value.

14.  $f(x) = 6x + 9$ ; 3

15.  $g(x) = -x + 5$ ; 2

16.  $h(x) = -7x + 12$ ; -9

17.  $j(x) = 4x + 11$ ; -13

18.  $m(x) = 9x - 5$ ; -2

19.  $n(x) = -2x - 21$ ; -6

20.  $p(x) = -12x - 36$ ; -3

21.  $q(x) = 8x - 32$ ; -4

22. ★ **MULTIPLE CHOICE** What value of  $x$  makes  $f(x) = 5$  if  $f(x) = -2x + 25$ ?

- (A) -15      (B) -10      (C) 10      (D) 15

**EXAMPLE 4**

on p. 264  
for Exs. 23–34

**TRANSFORMATIONS OF LINEAR FUNCTIONS** Graph the function. Compare the graph with the graph of  $f(x) = x$ .

23.  $g(x) = x + 5$

24.  $h(x) = 6 + x$

25.  $q(x) = x - 1$

26.  $m(x) = x - 6$

27.  $d(x) = x + 7$

28.  $t(x) = x - 3$

29.  $r(x) = 4x$

30.  $w(x) = 5x$

31.  $h(x) = -3x$

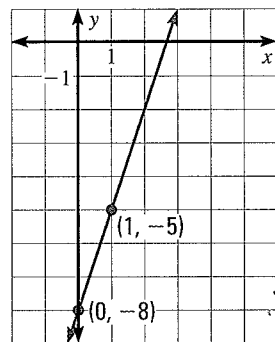
32.  $k(x) = -6x$

33.  $g(x) = \frac{1}{3}x$

34.  $m(x) = -\frac{7}{2}x$

35. ★ **MULTIPLE CHOICE** The graph of which function is shown?

- (A)  $f(x) = 3x + 8$   
(B)  $f(x) = 3x - 8$   
(C)  $f(x) = 8x + 3$   
(D)  $f(x) = 8x - 3$



36. ★ **OPEN-ENDED** In this exercise you will compare the graphs of linear functions when their slopes and  $y$ -intercepts are changed.

- Choose a linear function of the form  $f(x) = mx + b$  where  $m \neq 0$ . Then graph the function.
- Using the same  $m$  and  $b$  values as in part (a), graph the function  $g(x) = 2mx + b$ . How are the slope and  $y$ -intercept of the graph of  $g$  related to the slope and  $y$ -intercept of the graph of  $f$ ?
- Using the same  $m$  and  $b$  values as in part (a), graph the function  $h(x) = mx + (b - 3)$ . How are the slope and  $y$ -intercept of the graph of  $h$  related to the slope and  $y$ -intercept of the graph of  $f$ ?

37. **REASONING** How is the graph of  $g(x) = 1$  related to the graph of  $h(x) = -1$ ?

38. **CHALLENGE** Suppose that  $f(x) = 4x + 7$  and  $g(x) = 2x$ . What is a rule for  $g(f(x))$ ? What is a rule for  $f(g(x))$ ?

## PROBLEM SOLVING

**EXAMPLE 3**  
on p. 263  
for Exs. 39–41

- 39. MOVIE TICKETS** The average price of a movie ticket in the United States from 1980 to 2000 can be modeled by the function  $f(x) = 0.10x + 2.75$  where  $x$  is the number of years since 1980.

- Graph the function and identify its domain and range.
- Find the value of  $x$  so that  $f(x) = 4.55$ . *Explain* what the solution means in this situation.

**@HomeTutor** for problem solving help at classzone.com

- 40. DVD PLAYERS** The number (in thousands) of DVD players sold in the United States from 1998 to 2003 can be modeled by  $f(x) = 4250x + 330$  where  $x$  is the number of years since 1998.

- Graph the function and identify its domain and range.
- Find the value of  $x$  so that  $f(x) = 13,080$ . *Explain* what the solution means in this situation.

**@HomeTutor** for problem solving help at classzone.com

- 41. IN-LINE SKATING** An in-line skater's average speed is 10 miles per hour. The distance traveled after skating for  $x$  hours is given by the function  $d(x) = 10x$ . Graph the function and identify its domain and range. How long did it take the skater to travel 15 miles? *Explain*.

**Animated Algebra** at classzone.com



**EXAMPLE 5**  
on p. 265  
for Exs. 42–43

- 42. HOME SECURITY** A home security company charges new customers \$155 for the installation of security equipment and a monthly fee of \$40. To attract more customers, the company reduces its installation fee to \$75. The functions below give the total cost for  $x$  months of service:

**Regular fee:**  $f(x) = 40x + 155$       **Reduced fee:**  $g(x) = 40x + 75$

Graph both functions. How is the graph of  $g$  related to the graph of  $f$ ?

- 43. THEATERS** A ticket for a play at a theater costs \$16. The revenue (in dollars) generated from the sale of  $x$  tickets is given by  $s(x) = 16x$ . The theater managers raise the cost of tickets to \$20. The revenue generated from the sale of  $x$  tickets at that price is given by  $r(x) = 20x$ . Graph both functions. How is the graph of  $r$  related to the graph of  $s$ ?

- 44. ★ EXTENDED RESPONSE** The cost of supplies, such as mustard and napkins, a pretzel vendor needs for one day is \$75. Each pretzel costs the vendor \$.50 to make. The total daily cost to the vendor is given by  $C(x) = 0.5x + 75$  where  $x$  is the number of pretzels the vendor makes.

- Graph** Graph the cost function.
- Graph** The vendor sells each pretzel for \$3. The revenue is given by  $R(x) = 3x$  where  $x$  is the number of pretzels sold. Graph the function.
- Explain** The vendor's profit is the difference of the revenue and the cost. *Explain* how you could use the graphs to find the vendor's profit for any given number of pretzels made and sold.

45. ★ **EXTENDED RESPONSE** The number of hours of daylight in Austin, Texas, during the month of March can be modeled by the function  $l(x) = 0.03x + 11.5$  where  $x$  is the day of the month.
- Graph** Graph the function and identify its domain and range.
  - Graph** The number of hours of darkness can be modeled by the function  $d(x) = 24 - l(x)$ . Graph the function on the same coordinate plane as you used in part (a). Identify its domain and range.
  - CHALLENGE** Explain how you could have obtained the graph of  $d$  from the graph of  $l$  using translations and reflections.
  - CHALLENGE** What does the point where the graphs intersect mean in terms of the number of hours of daylight and darkness?

### MIXED REVIEW

Solve the equation or proportion.

46.  $y - 7 = -3$  (p. 134)      47.  $4.5m = 49.5$  (p. 134)      48.  $4z + 5z = -36$  (p. 141)
49.  $5(x - 4) = 20$  (p. 148)      50.  $3t + 4 + 5t = -4$  (p. 148)      51.  $-5g = 3(g - 8)$  (p. 154)
52.  $9n = 4(2n + 1)$  (p. 154)      53.  $\frac{7}{6} = \frac{t}{42}$  (p. 168)      54.  $\frac{5}{6} = \frac{p}{15}$  (p. 168)

Write the equation in slope-intercept form. Then graph the equation. (p. 244)

55.  $x + 6y = 12$       56.  $5x + y = -10$       57.  $2x - 2y = 3$
58.  $-2x - 3y = 21$       59.  $-4x - 3y = -18$       60.  $2x - y = 10$

#### PREVIEW

Prepare for  
Lesson 5.1 in  
Exs. 55–60.

### QUIZ for Lessons 4.6–4.7

Given that  $y$  varies directly with  $x$ , use the specified values to write a direct variation equation that relates  $x$  and  $y$ . (p. 253)

1.  $x = 5, y = 10$       2.  $x = 4, y = 6$       3.  $x = 2, y = -16$

Evaluate the function. (p. 262)

4.  $g(x) = 6x - 5$  when  $x = 4$       5.  $h(x) = 14x + 7$  when  $x = 2$
6.  $j(x) = 0.2x + 12.2$  when  $x = 244$       7.  $k(x) = \frac{5}{6}x + \frac{1}{3}$  when  $x = 4$

Graph the function. Compare the graph to the graph of  $f(x) = x$ . (p. 262)

8.  $g(x) = -4x$       9.  $h(x) = x - 2$

10. **HOURLY WAGE** The table shows the number of hours that you worked for each of three weeks and the amount that you were paid. What is your hourly wage? (p. 253)

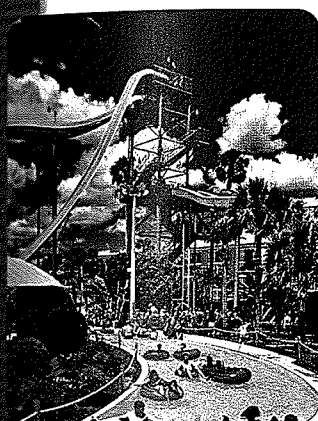
Hours	12	16	14
Pay (dollars)	84	112	98



## Lessons 4.4–4.7

- MULTI-STEP PROBLEM** The amount of drink mix  $d$  (in tablespoons) that you need to add to  $w$  fluid ounces of water is given by  $d = \frac{1}{4}w$ .
  - Graph the equation.
  - Use the graph to find the amount of drink mix you need if you want to make enough drinks to serve 4 people. Assume 1 serving is 8 fluid ounces.

- MULTI-STEP PROBLEM** A water park charges \$25 per ticket for adults. Let  $s$  be the amount of money the park receives from adult ticket sales, and let  $t$  be the number of adult tickets sold.
  - Write a direct variation equation that relates  $t$  and  $s$ .
  - How much money does the park earn when 90 adult tickets are sold?
  - The park collected \$3325 in adult ticket sales in one day. How many tickets did the park sell?



- SHORT RESPONSE** You and your friend are each reading an essay that is 10 pages long. You read at a rate of 1 page per minute. Your friend reads at a rate of  $\frac{2}{3}$  page per minute. The models below give the number  $p$  of pages you and your friend have left to read after reading for  $m$  minutes.
 

**You:**  $p = -m + 10$

**Your friend:**  $p = -\frac{2}{3}m + 10$

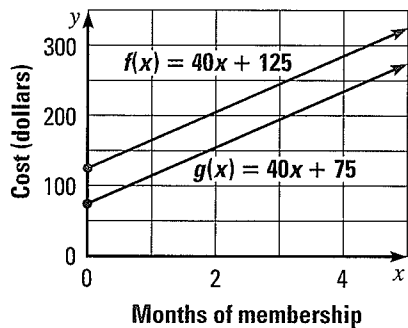
Graph both equations in the same coordinate plane. *Explain* how you can use the graphs to find how many more minutes it took your friend to read the essay than it took you to read the essay.

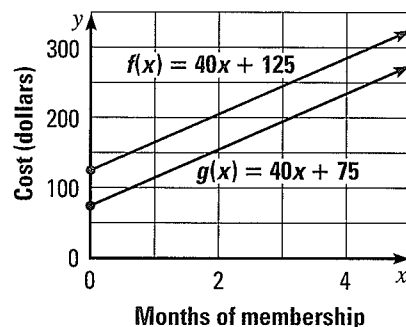
- OPEN-ENDED** Draw a graph that represents going to a movie theater, watching a movie, and returning home from the theater. Let the  $x$ -axis represent time and the  $y$ -axis represent your distance from home.

- EXTENDED RESPONSE** A central observatory averages and then reports the number of sunspots recorded by various observatories. The table shows the average number of sunspots reported by the central observatory in years since 1995.
 

Years since 1995	Average number of sunspots
0	17.5
2	21.0
4	93.2
6	110.9

  - Draw a line graph of the data.
  - During which two-year period was the increase in sunspots the greatest? Find the rate of change for this time period.
  - During which two-year period was the increase in sunspots the least? Find the rate of change for this time period.
  - Explain* how you could find the overall rate of change for the time period shown.

- GRIDDED ANSWER** To become a member at a gym, you have to pay a sign-up fee of \$125 and a monthly fee of \$40. To attract new customers, the gym lowers the sign-up fee to \$75. The function  $f$  gives the total cost with the regular sign-up fee. The function  $g$  gives the total cost with the reduced sign-up fee. The graphs of  $f$  and  $g$  are shown. The graph of  $g$  is a vertical translation of the graph of  $f$  by how many units down?
 





## BIG IDEAS

## For Your Notebook

## Big Idea ①

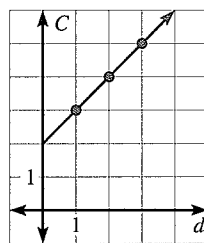
## Graphing Linear Equations and Functions Using a Variety of Methods

You can graph a linear equation or function by making a table, using intercepts, or using the slope and  $y$ -intercept.

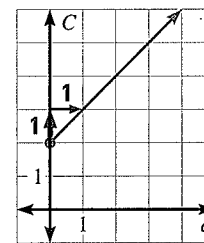
A taxi company charges a \$2 fee to pick up a customer plus \$1 per mile to drive to the customer's destination. The total cost  $C$  (in dollars) that a customer pays to travel  $d$  miles is given by  $C = d + 2$ . Graph this function.

Method: Make a table.

$d$	$C$
0	2
1	3
2	4
3	5



Method: Use slope and  $C$ -intercept.



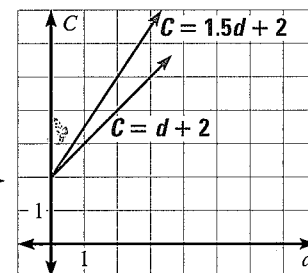
## Big Idea ②

## Recognizing How Changes in Linear Equations and Functions Affect Their Graphs

When you change the value of  $m$  or  $b$  in the equation  $y = mx + b$ , you produce an equation whose graph is related to the graph of the original equation.

Suppose the taxi company raises its rate to \$1.50 per mile. The total amount that a customer pays is given by  $C = 1.5d + 2$ . Graph the function.

You can see that the graphs have the same  $C$ -intercept, but different slopes.

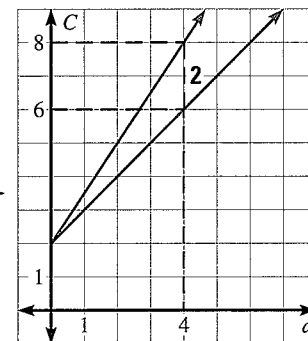


## Big Idea ③

## Using Graphs of Linear Equations and Functions to Solve Real-world Problems

You can use the graphs of  $C = d + 2$  and  $C = 1.5d + 2$  to find out how much more a customer pays to travel 4 miles at the new rate than at the old rate.

A customer pays \$2 more to travel 4 miles at the new rate.



## REVIEW KEY VOCABULARY

- quadrant, p. 206
- solution of an equation in two variables, p. 215
- graph of an equation in two variables, p. 215
- linear equation, p. 216
- standard form of a linear equation, p. 216
- linear function, p. 217
- x-intercept, p. 225
- y-intercept, p. 225
- slope, p. 235
- rate of change, p. 237
- slope-intercept form, p. 244
- parallel, p. 246
- direct variation, p. 253
- constant of variation, p. 253
- function notation, p. 262
- family of functions, p. 263
- parent linear function, p. 263

### VOCABULARY EXERCISES

1. Copy and complete: The ? of a nonvertical line is the ratio of vertical change to horizontal change.
2. Copy and complete: When you write  $y = 2x + 3$  as  $f(x) = 2x + 3$ , you use ?.
3. **WRITING** Describe three different methods you could use to graph the equation  $5x + 3y = 12$ .
4. Tell whether the equation is written in slope-intercept form. If the equation is not in slope-intercept form, write it in slope-intercept form.
  - a.  $3x + y = 6$
  - b.  $y = 5x + 2$
  - c.  $x = 4y - 1$
  - d.  $y = -x + 6$

## REVIEW EXAMPLES AND EXERCISES

Use the review examples and exercises below to check your understanding of the concepts you have learned in each lesson of Chapter 4.

### 4.1

### Plot Points in a Coordinate Plane

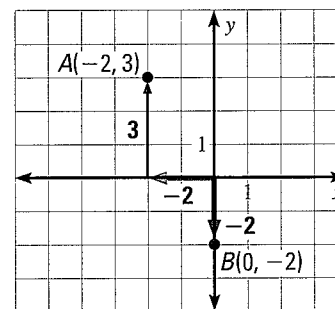
pp. 206–212

#### EXAMPLE

Plot the points  $A(-2, 3)$  and  $B(0, -2)$  in a coordinate plane. Describe the location of the points.

Point  $A(-2, 3)$ : Begin at the origin and move 2 units to the left, then 3 units up. Point  $A$  is in Quadrant II.

Point  $B(0, -2)$ : Begin at the origin and move 2 units down. Point  $B$  is on the y-axis.



#### EXERCISES

Plot the point in a coordinate plane. Describe the location of the point.

5.  $A(3, 4)$
6.  $B(-5, 0)$
7.  $C(-7, -2)$

EXAMPLE 2  
on p. 207  
for Exs. 5–7

## 4.2 Graph Linear Equations

pp. 215–221

## EXAMPLE

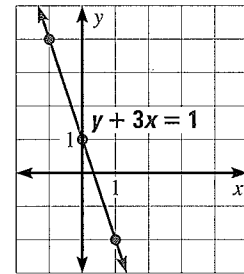
Graph the equation  $y + 3x = 1$ .**STEP 1** Solve the equation for  $y$ .

$$y + 3x = 1$$

$$y = -3x + 1$$

**STEP 2** Make a table by choosing a few values for  $x$  and finding the values for  $y$ .

$x$	-1	0	1
$y$	4	1	-2

**STEP 3** Plot the points.**STEP 4** Connect the points by drawing a line through them.

**EXAMPLE 2**  
on p. 216  
for Exs. 8–10

## EXERCISES

Graph the equation.

8.  $y + 5x = -5$

9.  $2x + 3y = 9$

10.  $2y - 14 = 4$

## 4.3 Graph Using Intercepts

pp. 225–232

## EXAMPLE

Graph the equation  $-0.5x + 2y = 4$ .**STEP 1** Find the intercepts.

$$-0.5x + 2y = 4$$

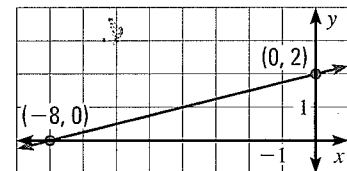
$$-0.5x + 2y = 4$$

$$-0.5x + 2(0) = 4$$

$$-0.5(0) + 2y = 4$$

$$x = -8 \leftarrow x\text{-intercept}$$

$$y = 2 \leftarrow y\text{-intercept}$$

**STEP 2** Plot the points that correspond to the intercepts:  $(-8, 0)$  and  $(0, 2)$ .**STEP 3** Connect the points by drawing a line through them.

## EXERCISES

Graph the equation.

11.  $-x + 5y = 15$

12.  $4x + 4y = -16$

13.  $2x - 6y = 18$

14. **CRAFT FAIR** You sell necklaces for \$10 and bracelets for \$5 at a craft fair. You want to earn \$50. This situation is modeled by the equation  $10n + 5b = 50$  where  $n$  is the number of necklaces you sell and  $b$  is the number of bracelets you sell. Find the intercepts of the graph of the equation. Then graph the equation. Give three possibilities for the number of bracelets and necklaces that you could sell.

**EXAMPLES 2 and 4**  
on pp. 226–227  
for Exs. 11–14

## 4.4 Find Slope and Rate of Change

pp. 235–242

### EXAMPLE

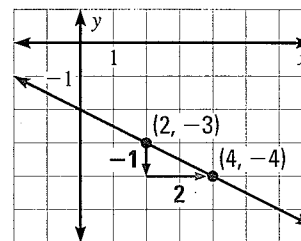
Find the slope of the line shown.

Let  $(x_1, y_1) = (2, -3)$  and  $(x_2, y_2) = (4, -4)$ .

$$m = \frac{y_2 - y_1}{x_2 - x_1} \quad \text{Write formula for slope.}$$

$$= \frac{-4 - (-3)}{4 - 2} \quad \text{Substitute values.}$$

$$= -\frac{1}{2} \quad \text{Simplify.}$$



EXAMPLES  
1, 2, 3, and 4  
on pp. 235–236  
for Exs. 15–17

### EXERCISES

Find the slope of the line that passes through the points.

15.  $(-1, 11)$  and  $(2, 10)$       16.  $(-2, 0)$  and  $(4, 9)$       17.  $(-5, 4)$  and  $(1, -8)$

## 4.5 Graph Using Slope-Intercept Form

pp. 244–250

### EXAMPLE

Graph the equation  $2x + y = -1$ .

**STEP 1** Rewrite the equation in slope-intercept form.

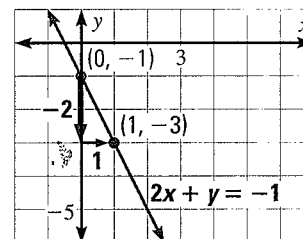
$$2x + y = -1 \rightarrow y = -2x - 1$$

**STEP 2** Identify the slope and the  $y$ -intercept.

$$m = -2 \text{ and } b = -1$$

**STEP 3** Plot the point that corresponds to the  $y$ -intercept,  $(0, -1)$ .

**STEP 4** Use the slope to locate a second point on the line.  
Draw a line through the two points.



EXAMPLES  
2 and 3  
on p. 245  
for Exs. 18–21

### EXERCISES

Graph the equation.

18.  $4x - y = 3$       19.  $3x - 6y = 9$       20.  $-3x + 4y - 12 = 0$

21. **RUNNING** One athlete can run a 60 meter race at an average rate of 7 meters per second. A second athlete can run the race at an average rate of 6 meters per second. The distance  $d$  (in meters) the athletes have left to run after  $t$  seconds is given by the following equations:

**Athlete 1:**  $d = -7t + 60$

**Athlete 2:**  $d = -6t + 60$

Graph both models in the same coordinate plane. About how many seconds faster does the first athlete finish the race than the second athlete?

## 4

## CHAPTER REVIEW

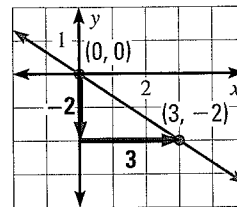
## 4.6 Model Direct Variation

pp. 253–259

## EXAMPLE

Graph the direct variation equation  $y = -\frac{2}{3}x$ .

Plot a point at the origin. The slope is equal to the constant of variation,  $-\frac{2}{3}$ . Find and plot a second point, then draw a line through the points.



## EXERCISES

Tell whether the equation represents direct variation. If so, identify the constant of variation.

22.  $x - y = 3$

23.  $x + 2y = 0$

24.  $8x - 2y = 0$

Graph the direct variation equation.

25.  $y = 4x$

26.  $-5y = 3x$

27.  $4x + 3y = 0$

28. **SNOWSTORMS** The amount  $s$  (in inches) of snow that fell during a snowstorm varied directly with the duration  $d$  (in hours) of the storm. In the first 2 hours of the storm 5 inches of snow fell. Write a direct variation equation that relates  $d$  and  $s$ . How many inches of snow fell in 6 hours?

## EXAMPLES

1, 2, and 4

on pp. 253–255  
for Exs. 22–28

## 4.7 Graph Linear Functions

pp. 262–268

## EXAMPLE

Evaluate the function  $f(x) = -6x + 5$  when  $x = 3$ .

$$f(x) = -6x + 5 \quad \text{Write function.}$$

$$f(3) = -6(3) + 5 \quad \text{Substitute 3 for } x.$$

$$= -13 \quad \text{Simplify.}$$

## EXERCISES

Evaluate the function.

29.  $g(x) = 2x - 3$  when  $x = 7$

30.  $h(x) = -\frac{1}{2}x - 7$  when  $x = -6$

Graph the function. Compare the graph with the graph of  $f(x) = x$ .

31.  $j(x) = x - 6$

32.  $k(x) = -2.5x$

33.  $t(x) = 2x + 1$

34. **MOUNT EVEREST** Mount Everest is rising at a rate of 2.4 inches per year. The number of inches that Mount Everest rises in  $x$  years is given by the function  $f(x) = 2.4x$ . Graph the function and identify its domain and range. Find the value of  $x$  so that  $f(x) = 250$ . Explain what the solution means in this situation.

## EXAMPLES

1 and 3

on pp. 262–263  
for Exs. 29–34

Plot the point in a coordinate plane. *Describe* the location of the point.

1.  $A(7, 1)$                       2.  $B(-4, 0)$                       3.  $C(3, -9)$

Draw the line that has the given intercepts.

4.  $x$ -intercept: 2  
 $y$ -intercept: -6                      5.  $x$ -intercept: -1  
 $y$ -intercept: 8                      6.  $x$ -intercept: -3  
 $y$ -intercept: -5

Find the slope of the line that passes through the points.

7.  $(2, 1)$  and  $(8, 4)$                       8.  $(-2, 7)$  and  $(0, -1)$                       9.  $(3, 5)$  and  $(3, 14)$

Identify the slope and  $y$ -intercept of the line with the given equation.

10.  $y = -\frac{3}{2}x - 10$                       11.  $7x + 2y = -28$                       12.  $3x - 8y = 48$

Tell whether the equation represents direct variation. If so, identify the constant of variation.

13.  $x + 4y = 4$                       14.  $-\frac{1}{3}x - y = 0$                       15.  $3x - 3y = 0$

Graph the equation.

16.  $x = 3$                       17.  $y + x = 6$                       18.  $2x + 8y = -32$

Evaluate the function for the given value.

19.  $f(x) = -4x$  when  $x = 2.5$                       20.  $g(x) = \frac{5}{2}x - 6$  when  $x = -2$

21. **BUSINESS** To start a dog washing business, you invest \$300 in supplies. You charge \$10 per hour for your services. Your profit  $P$  (in dollars) for working  $t$  hours is given by  $P = 10t - 300$ . Graph the equation. You will break even when your profit is \$0. Use the graph to find the number of hours you must work in order to break even.

22. **PEDIATRICS** The dose  $d$  (in milligrams) of a particular medicine that a pediatrician prescribes for a patient varies directly with the patient's mass  $m$  (in kilograms). The pediatrician recommends a dose of 150 mg of medicine for a patient whose mass is 30 kg.

- a. Write a direct variation equation that relates  $m$  and  $d$ .  
b. What would the dose of medicine be for a patient whose mass is 50 kg?

23. **SCISSOR LIFT** The scissor lift is a device that can lower and raise a platform. The maximum and minimum heights of the platform of a particular scissor lift are shown. The scissor lift can raise the platform at a rate of 3.5 inches per second. The height of the platform after  $t$  seconds is given by  $h(t) = 3.5t + 48$ . Graph the function and identify its domain and range.

